

The part of Fermat's theorem

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Abstract:We can't have an equation where the left hand side is $4(2C+1)$ and the right hand side is $8C$.The more detailed properties of odd and even numbers will be covered later in this article.What's important is that when a number or an equation maintains certain properties about odd and even numbers. It will be difficult and there may be no other way to solve it.

Keywords:Basic math.odd number and even number.Untenable equation

Make $M \cdot 2^n = (n) \quad M$ is odd.So let's call that O
 $(2n+1)^2 = 4n(n+1)+1 = 8C+1$ Any odd number to the second power is $8C+1$
Extension $a^k = 4kC+1$ when a is odd and k is even.In fact, $a^k = 4 \cdot 2^d C + 1 \quad k = (d)$.
 $a^2 + b^2 - 2 = 16C$ when $a+b=8C$ a, b are odd.
Let $a=8C+1 \quad b=8C-1$ or $a=8C+3 \quad b=8C-3$ Equation was set up
There must be an even number of terms in the equation, and the O of these terms is the lowest and the same.
So,We omit the higher term of O . Just verify that it's big enough at the end.
If $8k$ and $8k^2$ appear, $8k^2$ can be ignored when k is even.

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 $X^m + Y^m = A^m$

When X plus Y has no divisor with m

We can get the following properties

$X^m + Y^m = (X+Y)Z^m \quad (X, Y, Z, m \text{ is odd})$

$X+Y = (\geq 3) \quad (\text{by } m \geq 3)$

$Z^m = X^{m-1} - X^{m-2}Y + \dots - XY^{m-2} + Y^{m-1}$

$Z^m = X^{m-1} - X^{m-2}Y + \dots - XY^{m-2} + Y^{m-1} = (X+Y)C + mY^{m-1}$

Since m is odd, m minus 1 is even

$Y^{m-1} - 1 = (\geq 3)$

When $X+Y = (\geq 3)$

$Z^m - m = (\geq 3)$

Known m is odd

Easy to know

$m = 4k+1. \quad \text{When } Z = 4n+1$

$m = 4k+3. \quad \text{When } Z = 4n+3$

(note: when $m=4k+1 \quad z=4k+3$, $Z^m - m = (1)$. $m=4k+3 \quad z=4k+1$ are in same way)

Known

$2Z^m - X^{m-1} - Y^{m-1} = (X-Y)^2(X^{m-3} + X^{m-5}Y^2 + \dots + X^2Y^{m-5} + Y^{m-3}) \dots \dots \dots (1)$

$2(Z^m - 1) + 1 - X^{m-1} + 1 - Y^{m-1} = (X-Y)^2(X^{m-3} + X^{m-5}Y^2 + \dots + X^2Y^{m-5} + Y^{m-3})$

$X+Y = (\geq 3) \quad \textcircled{1}$

Know $X-Y = (1) \quad \textcircled{2} \quad (\text{note } X, Y \text{ are odd})$

By $Z=4n+1$ m is odd

The left-hand side is (≥ 3), and the right-hand side is (2).

Invalid

When $Z=4n+3$, $m=4k+3$

After that, it's easy to find out about the nature of the n , k , Z , m , X , Y .

$$Z^m+1=4(n+1)(1-Z+Z^2-\dots+Z^{m-1})=4(n+1)(4k+3-(Z+1)+(Z^2-1)-(Z^3+1)+\dots+(Z^{m-1}-1))=4(n+1)((1+Z)C+4k+3)=4(n+1)(4C-1) \textcircled{3}$$

We want to determine the fundamental properties of X , Y , n , and k

$$\begin{aligned} & (\\ Z^m &= X^{m-1}-X^{m-2}Y+\dots-XY^{m-2}+Y^{m-1}=(X+Y)C+mY^{m-1} \\ & \dots+4n(4k+3)3^{4k+2}+3^{4k+3}-4k-3=(X+Y)C+m(Y^{m-1}-1) \end{aligned}$$

Let's assume the right-hand side is big enough to O

In this solution, even if the value of the current X and Y combination is small after the O operation, we can assume that it is large. In this way, if it is wrong, it is regarded as an error, and if it is correct, it proves that the O operation value of X and Y is very large.

$$\dots+4n3^{4k+3}+3^{4k+3}-4k-3(\geq 4)$$

So $n+k+2(\geq 2)$

So $n=(1)$ $k(\geq 2)$ or $n(\geq 2)$ $k=(1)$

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The following proves that $n(\geq 1)$

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We can be sure that $Z^m=\dots$ is now fully established.

So, we use Z^{2m} . This is a general approach.

Because there are many proofs here, for unnecessary trouble, it is necessary to reduce the unknown.

You must ensure that there is a correspondence between Z^m and X^{m-1} , Y^{m-1} such as, Z^m-Y^{m-1} , $Z^{m-1}+Y^{m-1}-1+2$.

Because we only know

$$"2Z^m-X^{m-1}-Y^{m-1}=(X-Y)^2(X^{m-3}+X^{m-5}Y^2+\dots+X^2Y^{m-5}+Y^{m-3})"$$

So $(2Z^m-X^{m-1}-Y^{m-1})(2Z^m+X^{m-1}+Y^{m-1})$ is best choice.

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$$\begin{aligned} & (2Z^m-X^{m-1}-Y^{m-1})(2Z^m+X^{m-1}+Y^{m-1})=4Z^{2m}-(X^{m-1}+Y^{m-1}-2)^2+4(X^{m-1}+Y^{m-1}-2)-4 \\ & 4(2C+1)(-8(n+1)+X^{m-1}+Y^{m-1}-2+32C)=4*3^{8k+6}+4*4n*(8k+6)*3^{8k+5}+4*(4k+3)(8 \\ & k+5)*16n^2*3^{8k+4}+\dots-4+4(X^{m-1}+Y^{m-1}-2)+128C \end{aligned}$$

$$4(2C+1)(-8(n+1)+32C+X^{m-1}+Y^{m-1}-2)=4*3^6-32n+64(4k+3)(8k+5)n^2*3^{8k+4}+\dots-4+4(X^{m-1}+Y^{m-1}-2)+128C$$

$$4(2C+1)(-8(n+1)+32C+X^{m-1}+Y^{m-1}-2)=-32-32n+4(X^{m-1}+Y^{m-1}-2)+128C+64(4k+3)(8k+5)n^2*3^{8k+4}$$

By $X+Y(\geq 3)$ ①

Know $(X^{m-1}+Y^{m-1}-2)(\geq 4)$

So $n(\geq 1)$ (2)

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Before that, I did n't know what the result would be. I did n't know my goal.

I could only get it closer to my goals. Of course, there must be $(4n+3)^{8k+6} = \dots + 4n(8k+6)3^{8k+5} + 3^{8k+6}$ in the process. In response to use Z^{2m}

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N is determined, and there are no other properties

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There are also many proofs below. We deliberately make $4-2X^{m-1}-2Y^{m-1}$ appear in the equation. Found that it is beneficial to increase the value of the O operation result of $4-2X^{m-1}-2Y^{m-1}$. Because one of our purposes is to increase the value of the O operation of a known item. when $a+b=5$, because $a = (1) b = (1)$ is true, when the O operation value of b increases, that is, $b = (2)$ is not true and we are happy to see it.

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$$(2Z^m + X^{m-1} + Y^{m-1} - 4)(2Z^m + X^{m-1} + Y^{m-1}) = 4Z^{2m} - 4 + 2(Z^m + 1)(X^{m-1} + Y^{m-1} - 2) + (X^{m-1} + Y^{m-1} - 2)^2 + 4 - 2X^{m-1} - 2Y^{m-1}$$

(by when $a+b=8C \quad a^2+b^2-2=16C$)

$$32(2C+1) = 4(3^{8k+6} - 1) + 4 - 2X^{m-1} - 2Y^{m-1} + 64C$$

$$32(2C+1) = 4(3^6 - 1) + 4 - 2X^{m-1} - 2Y^{m-1} + 64C$$

$$32(2C+1) = 4(3^2 - 1) + 4 - 2X^{m-1} - 2Y^{m-1} + 64C$$

$$X^{m-1} + Y^{m-1} - 2 = (>=5) \quad (3)$$

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I did not expect such a result. Regarding the result, we can only choose a new equation. Because the original equation can no longer produce new results. And the new equation does not necessarily have a considerable result. Just like before, use Z^{2m} is to add a new equation. I have tried many times to get these valuable equations.

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 $X^{m-1} + Y^{m-1} - 2$ is determined, and there are no other properties

$$4XY(X^{m-3} + X^{m-5}Y^2 + \dots)$$

$$+ X^2Y^{m-5} + Y^{m-3} + 4Z^m - 2(Z^m + 1) = 4(X^{m-1} + X^{m-3}Y^2 + \dots + Y^{m-1}) - 2(Z^m + 1)$$

$$\text{By } \textcircled{3} \text{ and } X^{m-1} = 8C + 1 \quad X^{m-3}Y^2 = 8C + 1 \quad \dots$$

$$= 32C + 8k + 8n + 16$$

$$4XY(X^{m-3} + X^{m-5}Y^2 + \dots)$$

$$+ X^2Y^{m-5} + Y^{m-3} + 4Z^m - 2(Z^m + 1) = 4XY(X^{m-3} + X^{m-5}Y^2 + \dots)$$

$$+ X^2Y^{m-5} + Y^{m-3} + X^{m-1} + Y^{m-1} - 2 + (2Z^m - X^{m-1} - Y^{m-1})$$

$$= 4XY(X^{m-3} + X^{m-5}Y^2 + \dots)$$

$$+ X^2Y^{m-5} + Y^{m-3} + X^{m-1} + Y^{m-1} - 2 + (X - Y)^2(X^{m-3} + X^{m-5}Y^2 + \dots + X^2Y^{m-5} + Y^{m-3})$$

$$= (X + Y)^2(X^{m-3} + X^{m-5}Y^2 + \dots + X^2Y^{m-5} + Y^{m-3}) + X^{m-1} + Y^{m-1} - 2 = (>=5)$$

In addition

$$4XY(X^{m-3} + X^{m-5}Y^2 + \dots)$$

$$+ X^2Y^{m-5} + Y^{m-3} + 4Z^m - 2(Z^m + 1) = 4(X^{m-1} + X^{m-3}Y^2 + \dots + Y^{m-1}) - 2(Z^m + 1)$$

$$= 32C + 8k + 8n + 16$$

$$32C + 8k + 8n + 16 = (>=5)$$

$$k + n = (1)$$

$$\text{By } \textcircled{2} \quad n = (>=1)$$

$k \geq 1$)

k is determined, and there are no other properties

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This is exactly what we imagined before. $Z^m = X^{m-1} - X^{m-2}Y + \dots$

$-XY^{m-2} + Y^{m-1}$ is used here. Or, n and k appears on the left side of the equation. The right side of the equation uses the known equation to find the result of its O operation.

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Know $n \geq 2$ $k = 1$ or $n \geq 1$ $k \geq 2$

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Now, start to find the attributes of X and Y . Because it is needed later. As I said before, suppose the value of the O operation of the X and Y items is large enough. Now, start to prove that the value of the operation O of X and Y is large enough.

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By (3) $X^{m-1} + Y^{m-1} - 2 \geq 5$

When X, Y are $16C-3, 16C+3$ or $16C+5, 16C-5$ or $16C+1, 16C+7$ or $16C-1, 16C-7$, X, Y do not meet $X^{m-1} + Y^{m-1} - 2 \geq 5$

Such as $X = 16C-3, X^{2k+1} = 16C - 3^{2k+1} = 16C - 3 + 3(1 - 3^{2k})$ by $k \geq 1, X^{2k+1} = 16C - 3 - X^{m-1} + Y^{m-1} - 2 = X^{4k+2} + Y^{4k+2} - 2 = (16C-3)^2 + (16C+3)^2 - 2 = 32C + 16$

So X, Y are $16C-1, 16C+1$ or $16C+7, 16C-7$ or $16C+3, 16C+5$ or $16C-3, 16C-5$

Know $XY = 16C - 1$

$Z^{m+1} = 4(n+1)(1 - Z + Z^2 + \dots + Z^{m-1}) = 4(n+1)(1 + Z^2 + \dots + Z^{m-1} - Z - Z^3 - \dots - Z^{m-2})$

$Z^{m+1} = 4(n+1)(8C + 2k + 2 - Z(2k+1)) = 4(n+1)(8C + 2k + 2 - (4n+3)(2k+1))$

By $n \geq 1$ $k \geq 1$

$Z^{m+1} = 32C - 4(n+1)$

Z^m is determined, and there are no other properties

$Z^{m+4n+5} = 64C + 4n \cdot 3^{4k+3} + 3^{4k+3} + 4n + 5 = 64C + 16n(2C+1) + 3^3(3^{4k}-1) + 32$

Science $n = 1$ $k \geq 2$ $16n(2C+1) = 32 + 64C$ $(3^{4k}-1) = 64C$

Science $n \geq 2$ $k = 1$ $16n(2C+1) = 64C$ $(3^{4k}-1) = 64C + 32$

So $Z^{m+4n+5} = 64C$

$Z^m = 64C - 4n - 5$

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This is also necessary because it can reduce the amount of subsequent calculations. In other words, $Z = -4n - 5$

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$2(X+Y)^2(X^{m-3} + X^{m-5}Y^2 + \dots + Y^{m-3})(-X^{m-1} - Y^{m-1}) =$

$-(4Z^m + 8XY(X^{m-3} + X^{m-5}Y^2 + \dots$

$+ Y^{m-3}))(Y^{m-1} - X^{m-1}) - 8X^{m-1}(X(X+Y)(X^{m-3} + X^{m-5}Y^2 + \dots$

$+ Y^{m-3})) + (Y^{m-1} - X^{m-1})^2 + 2(Y+X)^2(Y-X)^2(X^{m-3} + X^{m-5}Y^2 + \dots + Y^{m-3})^2$

$-(Z^m + 2XY(X^{m-3} + X^{m-5}Y^2 + \dots$

$$+Y^{m-3})(Y^{m-1}-X^{m-1})-2X^{m-1}(X(X+Y)(X^{m-3}+X^{m-5}Y^2+\dots+Y^{m-3}))=(D) \quad (4)$$

D is a big number

$$(Y^{m-1}-X^{m-1})=(Y-X)C$$

Here, $X-Y = 16C-2$ is used cleverly when $X = 16C-1$ or $X = 16C-7$

This is another new equation. Because at any time $Z^m=64C-4n-5$ will cause the equation to hold. However, m can be not given directly. X, Y can appear directly in any equation. However, X and Y are $16C-1, 16C+1$ C is an arbitrary number, so that the O operation value of a certain two items is very small. So, we have to consider -1 or -7 in $16C-1, 16C+1$ in X and Y instead of 16C

$$\begin{aligned} & ((64C+4n+5-2(16C-1)(8C+2k+1))(Y-X)((X^{2k}+X^{2k-2}Y^2+\dots \\ & +Y^{2k})^2-X^2Y^2(X^{2k-2}+X^{2k-4}Y^2+\dots \\ & +Y^{2k-2})^2-2(8C+1)(X(8C+2k+1)))(X+Y)=(D) \\ & ((64C+4n+5-2(16C-1)(8C+2k+1))(Y-X)((8C+k+1)^2-(8C+1)(8C+k)^2-2(8C+1) \\ & (X(8C+2k+1)))(X+Y)=(D) \\ & ((4n+5+2(2k+1))(Y-X)((k+1)^2-k^2)-2X(2k+1))=(\geq 4) \\ & ((4n+5+2(2k+1))(Y-X)-2X)=(\geq 4) \quad (5) \end{aligned}$$

X is $16C+5$ or $16C-3$

By $Y-X=16C-2$ and (5)

$$(4n+5+2(2k+1)+5)=(\geq 4)$$

$$(4n+5+2(2k+1)-3)=(\geq 4)$$

Invalid

X is $16C+7$ and Y is $16C-7$

$$Y-X=16C+2 \quad X^2=(16C+7)^2=16C+49=16C+1$$

By (4)

$$\begin{aligned} & -(Z^m+2XY(X^{m-3}+X^{m-5}Y^2+\dots \\ & +Y^{m-3}))+(Y^{m-1}-X^{m-1})-2X^{m-1}(X(X+Y)(X^{m-3}+X^{m-5}Y^2+\dots+Y^{m-3}))=(D) \end{aligned}$$

$$\begin{aligned} & ((64C+4n+5-2(16C-1)(8C+2k+1))(Y-X)((X^{2k}+X^{2k-2}Y^2+\dots \\ & +Y^{2k})^2-X^2Y^2(X^{2k-2}+X^{2k-4}Y^2+\dots \\ & +Y^{2k-2})^2-2(16C+1)(X(16C+2k+1)))(X+Y)=(D) \end{aligned}$$

$$((4n+5+2(2k+1))(Y-X)-2X)=(\geq 5)$$

$$(4n+5+2(2k+1)-7)=(\geq 5)$$

Invalid

So X is $16C+1$ or $16C-1$

Know $X+Y=(\geq 6)$ (by $4k+1$ is error so $m=5$ is error so $X+Y=(5)$ is error)

$$X=16C_1+1 \quad Y=16C_2-1 \quad \text{easy to know } C_1+C_2=(\geq 1) \quad \text{so } C_1-C_2=(\geq 1)$$

$$XY=32C-1$$

$$Z^m=X^{m-1}-X^{m-2}Y+\dots-X^m+Y^{m-1}$$

$$Z^m=(X+Y)C+mX^{m-1}$$

$$X \text{ is } 16C+1 \text{ or } 16C-1$$

$$\text{Easy to know } 4k+4n+8=32C \quad Z^m=64C-4n-5$$

$$(4n+3)(-1+Z^{m-1}+1)=Z^m$$

$$(4n+3)(1+(16n^2+24n+8)(2k+1+(16n^2+24n+8)((2k+1)k+8C)))=Z^m$$

$$\text{When } k=(1)$$

$$32+112n+48k+48n^2+144nk+3*32n^2+3*64k=Z^m+4n+5+512C$$

$$(4n+3)(1+(16n^2+24n+8)(2k+1+(16n^2+24n+8)((Z^2)^{2k-1}+2(Z^2)^{2k-2}+3(Z^2)^{2k-3}+\dots+2k)))=Z^m$$

$$(4n+3)(1+(16n^2+24n+8)(2k+1+(16n^2+24n+8)((16n^2+24n+9)^{2k-1}+2(16n^2+24n+9)^{2k-2}+3(16n^2+24n+9)^{2k-3}+\dots+2k)))=Z^m$$

$$(4n+3)(1+(16n^2+24n+8)(2k+1+(16n^2+24n+8)((9)^{2k-1}+2(9)^{2k-2}+3(9)^{2k-3}+\dots+2k+16C)))=Z^m$$

$$(4n+3)(1+(16n^2+24n+8)(2k+1+(16n^2+24n+8)((9)+2+3(9)+4+5(9)+\dots+2k+16C)))=Z^m$$

$$(4n+3)(1+(16n^2+24n+8)(2k+1+(16n^2+24n+8)((9)k^2+k(k+1)+16C)))=Z^m$$

$$32+112n+48k+48n^2+144nk+3*32n^2+64n^3+3*64k(1+10k)=Z^m+4n+5+1024C$$

$$Z^m=X^{m-1}+Y^{m-1}-X^{m-2}Y-X^m+Y^{2k+1}$$

$$Z^m=(X+Y)^2C-(4k+3)X^{2k+1}Y^{2k+1}$$

$$XY=32C-1$$

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This shows that $Z^m+(4k+3)X^{2k+1}Y^{2k+1}$ cannot be very large after the O operation. Because $Z^m=(4n+3)^{4k+3}$ $k=(\geq 1)\dots\dots$

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When a,b,m is odd.

$$a^m+b^m=(a+b)(a^{m-1}+\dots\dots$$

$$+b^{m-1})=(a+b)(ma^{m-1}+(a+b)C)=(a+b)(m+4(m-1)C+(a+b)C)$$

$$\text{Because } a^{m-1}=4(m-1)C+1$$

So $a^m+b^m=(a+b)m+d$ The O operation of d is large, when the O operation of a+b is large

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$$1-3^{4k}=1-(4-1)^{4k}=16k-16*4k*(4k-1)/2+\dots\dots=16k+32k+\dots\dots$$

In future calculations, please keep more terms when expanding.

The next strategy is to use $a^m+(4k+3)^m(XY)^m=C$ to get $a+(4k+3)(XY)$. Use

$$(4k+3)(XY)=(4k+3)(XY)^{2k+1}+C \text{ and then change } (4k+3)(XY)^{2k+1} \text{ to}$$

$$(4n+3)^{4k+3}. \text{ In this process, there will be many single } k, n, nk.$$

First find $k=(\geq 2)$, then find that k has a large in O operation, and then

$$\text{substitute } (4n+3)^{8k+6}-(4k+3)^2(XY)^{4k+2}=2^{11}C$$

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($32nk \geq 8$) so $32nk = 256C$)

When $k=1$ $n \geq 2$ (this can reduce trouble)

$$3^{2k}(4n+3)^{4k+3} + 3^{2k}(4k+3)(XY)^{2k+1} = 256C$$

$$(4n+3)^{6k+3} + (4k+3)^{2k+1}(XY)^{2k+1} - 8nk + 8k^2 - 16k^3 = 256C$$

$$((4n+3)^3 + (4k+3)(XY))(2k+1) - 8nk + 8k^2 - 16k^3 = 256C$$

$$\text{By } (XY)^{2k} = 32C_1 \cdot 2k+1 = 64kC_1+1$$

$$((4n+3)^3 + (4k+3)(XY)^{2k+1})(2k+1) - 8nk + 8k^2 - 16k^3 + 64kC_1(2C+1) = 256C$$

$$\text{By } Z^m = (X+Y)^2C - (4k+3)X^{2k+1}Y^{2k+1}$$

$$((4n+3)^3 - Z^m)(2k+1) - 8nk + 8k^2 - 16k^3 + 64kC_1(2C+1) = 256C$$

$$\text{By } 32 + 112n + 48k + 48n^2 + 144nk + 3 \cdot 32n^2 + 64n^3 = 128 + Z^m + 4n + 5 + 256C \quad (k=1)$$

$$(-48k - 144nk)(2k+1) - 8nk + 8k^2 - 16k^3 + 128 + 64kC_1(2C+1) = 256C$$

$$8k(k-6) + 8nk + 64kC_1(2C+1) = 128 + 256C$$

$$8k(k+2) + 8nk + 64kC_1(2C+1) = 256C \quad (\text{appear } nk \text{ and the } O \text{ of it is small. It is goal})$$

$$(4n+3)^{4k+3} + (4k+3)(XY)^{2k+1} = 256C$$

$$16n^2(4n+3)^{4k+1} + 3(8n+3)(4n+3)^{4k+1} + (4k+3)^{2k+1}(XY)^{2k+1} - 3 \cdot 8k^2 - 3 \cdot 8k - 3 \cdot 16k = 256C$$

$$-4n \cdot 3 \cdot (4n+3)^{4k+1} + 16n^2(4n+3) + 3^2(4n+1)(4n+3)^{4k+1} + (4k+3)^{2k+1}(XY)^{2k+1} - 3 \cdot 8k^2 - 3 \cdot 8k - 3 \cdot 16k = 256C$$

$$-4n \cdot 3 \cdot (4n+3)^{4k+1} + 16n^2(4n+3) + 3^2(4n+1)^{2k+1}(4n+3)^{4k+1} + (4k+3)^{2k+1}(XY)^{2k+1} - 3 \cdot 8k^2 - 3 \cdot 8k - 3 \cdot 16k + 8nk = 256C$$

$$\text{By } 8k(k+2) + 8nk + 64kC_1(2C+1) = 256C$$

$$-4n \cdot 3 \cdot (4n+3)^{4k+1} + 16n^2(4n+3) + 3^2(4n+1)^{2k+1}(4n+3)^{4k+1} + (4k+3)^{2k+1}(XY)^{2k+1} - 32k^2 - 3 \cdot 8k - 64k = 256C + 64kC_1(2C+1)$$

$$-4n \cdot 3 \cdot (4n+3)^{4k+1} + 16n^2(4n+3) + 3^{4k+2}(4n+1)^{2k+1}(4n+3)^{4k+1} + (4k+3)^{2k+1}(XY)^{2k+1} - 3 \cdot 2k^2 - 3 \cdot 8k - 64k + 9(1 - (-4)^k)(4n+1)^{2k+1}(4n+3)^{4k+1} = 256C + 64kC_1(2C+1)$$

$$-4n \cdot 3 \cdot (4n+3)^{4k+1} + 16n^2(4n+3) + 3^{4k+2}(4n+1)^{2k+1}(4n+3)^{4k+1} + (4k+3)^{2k+1}(XY)^{2k+1} - 3 \cdot 2k^2 - 3 \cdot 8k - 64k + 3(16k + 32k) = 256C + 64kC_1(2C+1)$$

$$-4n \cdot 3 \cdot (4n+3)^{4k+1} + 16n^2(4n+3) + 3^{4k+2}(4n+1)^{2k+1}(4n+3)^{2k+1} + (4k+3)^{2k+1}(XY)^{2k+1} - 3 \cdot 2k^2 - 3 \cdot 8k - 16k - 3 \cdot 32k + 3^{4k+2}(4n+1)^{2k+1}(4n+3)^{2k+1}((4n+3)^{2k} - 1) = 256C + 64kC_1(2C+1)$$

$$-4n \cdot 3 \cdot (4n+3)^{4k+1} + 16n^2(4n+3) + 3^{4k+2}(4n+1)^{2k+1}(4n+3)^{2k+1} + (4k+3)^{2k+1}(XY)^{2k+1} - 3 \cdot 2k^2 - 3 \cdot 8k - 16k - 3 \cdot 32k + 5(8 \cdot nk + 8k + 16k - 32k^2) = 256C + 64kC_1(2C+1)$$

$$-4n \cdot 3 \cdot (4n+3)^{4k+1} + 16n^2(4n+3) + 3^{4k+2}(4n+1)^{2k+1}(4n+3)^{2k+1} + (4k+3)^{2k+1}(XY)^{2k+1} - 3 \cdot 32k + 5 \cdot 8 \cdot nk + 5 \cdot 16k = 256C + 64kC_1(2C+1)$$

$$-4n \cdot 3 \cdot (4n+3)^{4k+1} + 16n^2(4n+3) + (9(4n+1)(4n+3) + (4k+3)(XY))(2k+1) - 3 \cdot 32k + 5 \cdot 8 \cdot nk + 5 \cdot 16k = 256C + 64kC_1(2C+1)$$

$$-4n \cdot 3 \cdot (4n+3)^{4k+1} + 16n^2(4n+3) + (9(4n+1)(4n+3) + (4k+3)(XY)^{2k+1})(2k+1) - 3 \cdot 32k + 5 \cdot 8 \cdot nk + 5 \cdot 16k + 128kC = 256C$$

$$\text{By } Z^m = (X+Y)^2C - (4k+3)X^{2k+1}Y^{2k+1}$$

$$-4n \cdot 3^k (4n+3)^{4k+1} + 16n^2 (4n+3) + (9(4n+1)(4n+3) - Z^m)(2k+1) - 3 \cdot 32k + 5 \cdot 8 \cdot nk + 5 \cdot 16k = 256C$$

$$\text{By } 32 + 112n + 48k + 48n^2 + 144nk + 3 \cdot 32n^2 + 3 \cdot 64k = Z^m + 4n + 5 + 256C$$

$$-4n \cdot 3^k (4n+3) + 16n^2 (4n+3) + (9 \cdot 4n - 48k - 144nk - 3 \cdot 64k)(2k+1) - 3 \cdot 32k + 5 \cdot 8 \cdot nk + 5 \cdot 16k = 256C$$

$$-4n \cdot 3^k (4n+3) + 16n^2 (4n+3) + (-48k - 144nk)2k + 9 \cdot 4n = 256C$$

$$k \geq 2 \quad (\text{use } nk \text{ before it})$$

$$3^{3k} (4n+3)^{4k+3} + (4k+3)3^{3k} (XY)^{2k+1} = 1024C$$

$$(4n+3)^{3k} (4n+3)^{6k+2} + (4k+3)^{3k+1} (XY)^{3k+1} + 32kC + 4k^2 (2C+1) + 16k(2C+1) = 1024C$$

$$4n(4n+3)^{6k+2} + 3^{k+1} (4n+3)^{6k+2} + (4k+3)^{3k+1} (XY)^{3k+1} + 4k^2 (2C+1) + 16k(2C+1) + 32kC = 1024C$$

$$4n(4n+3)^2 + 3^{3k+1} (4n+3)^{6k+2} + (4k+3)^{3k+1} (XY)^{3k+1} + 32kC + 4k^2 (2C+1) + 3^k (1 - (4-1)^{2k}) (4n+3)^{6k+2} + 16k(2C+1) = 1024C$$

$$4n(4n+3)^2 + (3(4n+3)^2 + (4k+3)(XY))(3k+1 + 4k(2C+1)) + 128C + 4 \cdot 3k(3k+1)(2C+1) + 4k^2 (2C+1) + 8k + 16k + 32kC + 16k(2C+1) = 1024C$$

$$4n(4n+3)^2 + (3(4n+3)^2 + (4k+3)(XY)^{2k+1})(3k+1 + 4k(2C+1)) + 128C + 4k^2 (2C+1) + 8k + 32kC = 1024C$$

$$\text{By } Z^m = (X+Y)^2 C - (4k+3)X^{2k+1}Y^{2k+1}$$

$$4n(4n+3)^2 + (3(4n+3)^2 - Z^m)(3k+1 + 4k(2C+1)) + 128C + 4k^2 (2C+1) + 8k + 32kC = 1024C$$

$$\text{By } 32 + 112n + 48k + 48n^2 + 3 \cdot 32n^2 + 144nk + 64n^3 + 64kC = Z^m + 4n + 5 + 1024C \quad (\text{by } k \geq 4)$$

$$4n(4n+3)^2 + ((-9 \cdot 4n - 48k - 3 \cdot 32n^2 - 144nk - 64n^3 - 64kC)(3k+1 + 4k(2C+1)) + 128C) + 4k^2 (2C+1) + 8k + 32kC = 1024C$$

$$8k - 27 \cdot 4nk + 32kC - 48k + 4k^2 (2C+1) = 1024C$$

$$(3-8) \cdot 8k + 4nk + 32kC + 4k^2 (2C+1) = 1024C$$

$$3 \cdot 8k + 4nk + 32kC + 4k^2 (2C+1) = 1024C$$

$$\text{When } k=2$$

$$\text{By } 4n + 4k + 8 = 32C$$

$$n+2=2$$

$$n+6 \geq 3$$

$$(6+n)4k + 32kC + 4k^2 (2C+1) = 1024C$$

$$k \geq 3$$

$$\text{So } k \geq 6$$

$$Z^m = 3^{4k+3} + 4n(4k+3)3^{4k+2} + 16n^2(4k+3)(2k+1)3^{4k+1}$$

$$+ (4k+3)(2k+1)(4k+1)64n^3 3^{4k-1} + 2^{11}C$$

$$Z^m = 3^{4k+3} + 4n3^{4k+3} + 16n^2 3^{4k+2} + 64n^3 3^{4k} + 2^{11}C = 27 + 27 \cdot 4n + 9 \cdot 16n^2 + 64n^3 + 27 \cdot 16k + 2^{11}C$$

$$(4n+3)^{8k+6} - (4k+3)^2 (XY)^{4k+2} = 2^{11}C$$

$$3^{4k}(4n+3)^{8k+6}-3^{4k}(4k+3)^2(XY)^{4k+2}=2^{11}C$$

$$3^{4k}(16n^2+3*8n)(4n+3)^{8k+4}+3^{4k+2}(4n+3)^{8k+4}-(4k+3)^{4k+2}(XY)^{4k+2}=2^{11}C$$

$$(16n^2+3*8n)(4n+3)^4+(3(4n+3)^2+(4k+3)(XY))((4k+2)(3(4n+3)^2)^{4k+1}-(3(4n+3)^2+(4k+3)(XY))(8C+1))=2^{11}C$$

$$(16n^2+3*8n)(4n+3)^4+(3(4n+3)^2+(4k+3)(XY)^{2k+1})((4k+2)(3(4n+3)^2)^{4k+1}-(3(4n+3)^2+(4k+3)(XY)^{2k+1})(8C+1))=2^{11}C$$

By $Z^m=(X+Y)^2C-(4k+3)X^{2k+1}Y^{2k+1}$

$$(16n^2+3*8n)(4n+3)^4+(3(4n+3)^2-Z^m)((4k+2)(3(4n+3)^2)^{4k+1}-(3(4n+3)^2-Z^m)(8C+1))=2^{11}C$$

By $Z^m=27+27*4n+9*16n^2+64n^3+27*16k+2^{11}C$

$$(16n^2+3*8n)(4n+3)^4+(-9*4n-3*32n^2-64n^3-27*16k)(2(3(4n+3)^2)-(-9*4n-3*32n^2-64n^3-27*16k)(8C+1))=2^{11}C$$

(note: (8C+1) in it is result of operation)

$$-81*64n^2=(>=9)$$

Invalid

Refer to the introduction:

The manuscript is for the most part simple. Now let's look at some of the wrong things. And it can help us find the right way.

Refer to the content:

Let Y is even

$$X^N+Y^N=Z^N \quad X, Y, Z \text{ co-prime}$$

$$X^N=(Z^{N/2}+Y^{N/2})(Z^{N/2}-Y^{N/2}) \quad (Z^{N/2}+Y^{N/2}), (Z^{N/2}-Y^{N/2}) \text{ co-prime}$$

$N > 2$ $N = m/n$ m, n are odd

$$X_1^N = Z^{N/2} + Y^{N/2}$$

$$(X_1^{N/2} + Y^{N/4})(X_1^{N/2} - Y^{N/4}) = Z^{N/2}$$

$$X_1^{N/2} + Y^{N/4} = Z_1^{N/2}$$

In the same way

$$X_2^{N/4} + Y^{N/16} = Z_2^{N/4}$$

.....

$$\text{When } (a^{1/4} + b^{1/4})(a^{1/4} - b^{1/4})(a^{1/2} + b^{1/2}) = (1)$$

$$a^{1/4} - b^{1/4} = (1/4)$$

In addition

$$Z_1^{N/2} - X_1^{N/2} = (>= 1/2)$$

$$Y^{N/4} = (>= 1/2) \quad Y^N = (>= 2)$$

$$Z_2^{N/4} - X_2^{N/4} = (>= 1/4)$$

$$Y^{N/16} = (>= 1/4) \quad Y^N = (>= 4)$$

.....

Y^N infinite

When m, n are even, In the same way.

Now let's think about the following questions.

$$Z^m = (X+Y)^2C - (4k+3)X^{2k+1}Y^{2k+1}$$

$$(4n+3)^{4k+3} + (4k+3)X^{2k+1}Y^{2k+1} = (X+Y)^2C$$

We're going to use $A^{2C+1} + B^{2C+1} = (A+B)(2C+1)$ note $Z^m = 64C - 4n - 5$

In the above equation, A plus B is equal to (D), and D is large enough.

By $X^{2k+1}Y^{2k+1}$ It constrains $2C+1$ to be $2k+1$ or $4k+1$ or $6k+1$ or $8k+1$

Notice they're both $4C+1$ Rather than $4C-1$

When we expand parts of $(4n+3)^{4k+3}$, part of $(4n+3)^{4k+3}$ becomes part of A.

That part of $(4n+3)^{4k+3}$ is E. The other part is F.

By $A^{2C+1}+B^{2C+1}=(A+B)(4C+1)$

$E+(F+(4k+3)XY)(2C+1)=2^{11}C$

$E+(F-Z^m)(2C+1)=2^{11}C$

$E+F+4C(F-Z^m)-Z^m=2^{11}C$

$4C(F-Z^m)=2^{11}C$

So It doesn't make sense to change n. because $X^{2k+1}Y^{2k+1}$ constrains $2C+1$ to be $2k+1$ or $4k+1$ or $6k+1$ or $8k+1$

And we found that $k=(1)$ is always true.

Because, K is what we added. When we add a k , we definitely add a k^2 . Or k^*C is too big and meaningless. The way it came about was too simple.

Of course. $n*k$ is the product of change. What is remarkable is that it is chaotic. Unconstrained. We see it in many wrong cases. Each time, it's going to be an $8n*k$ one day, a $16n*k$ the next.

So there has to be a situation. It takes it out of the base case.

And then we need one that has k in it and it $=G$ G is low number.

And then we have to get out of the way.

Because the original formula is not going to get us what we want.

Because it's in this form,

$(4n+3)^3+(4k+3)X^{2k+1}Y^{2k+1}=(X+Y)^2C$

So if we still have a solution to this, we can definitely solve for X and Y .