

Grade 12 Students' Retention in Statistics and Probability amidst Covid-19

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Abstract This study aimed to assess the retention of grade 12 students in statistics and probability, along with a comparative analysis of these retentions across the distinct topics of the subject. Statistics and probability subjects were taken by the students when they were in grade 11. Employing a quantitative approach, the research used descriptive-comparative design to describe the level of retention of the students and compare the retention of the students in each topic. These encompass random variables and probability distribution, normal distribution, sampling and sampling distribution, and estimation parameters. The retention of the students studying at Nueva Vizcaya General Comprehensive High School, a public school in Nueva Vizcaya, Philippines was analyzed through the validated retention test administered to them. Using frequency count and percent, the result revealed that the grade 12 students' retention was described as "poor retention rate". Repeated-measures ANOVA confirmed that the retention of the students in all the topics are all poor. Hence, teachers should consider making an intervention to improve the retention of the students in statistics and probability. They may consider innovative ways to engage the students in learning. Also, the factors that influence the students in solving problems in designing the interventions.

Keywords: *random variables, probability distribution, normal distribution, sampling distribution, estimation parameters*

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1. Introduction

Statistics is the art of data learning. To understand more about something, gathering data should be done first. Statistics concerns the compilation of data, its subsequent description, interpretation, and drawing of conclusions [1]. But without applying probability theory, a student cannot appreciate the true essence of data analysis. Elements of probability help us infer with confidence. As such, probability principles are a major counterpart to statistical methods and allow one to measure the importance of statistics [2].

In the Philippines' K to 12 curriculum, statistics and probability is introduced as early as elementary years from Grade 1 to Grade 6 during the fourth quarter of the academic year [3]. For the secondary level, it is offered in the seventh, eighth, tenth, and eleventh grades. In the tenth grade of junior high school, the third and fourth quarters are allotted for teaching the subject. Thus, Grade 11 students take classes in this subject during the second half of the academic year regardless of the career track chosen. The integration of this subject aims to foster worldwide competitiveness and equip learners with mathematical skills. However, the first-ever participation of the Philippines in the Program for International Student

Assessment (PISA), showed that Filipino learners placed near last in science and mathematics among the 79 participating countries in the PISA [4,5]. Filipino students scored 353 points in mathematics against the 489 Organization for Economic Co-operation and Development (OECD) average [6]. In addition, the results of students in local examinations display low performance in mathematics. According to the Department of Education (DepEd) 2019-Year End Report regarding the National Achievement Test (NAT), the results displayed low proficiency levels, especially in science, English, and mathematics [7]. It is noted that NAT is administered for Grade 6, Grade 10, and Grade 12 students.

Addressing the challenges in mathematics education goes beyond understanding difficulties in learning the subject matter; it involves considering students' retention. Retention is needed to expand the cognitive abilities of children, logical thinking, self-sufficiency, and empowering memory, all of which are objectives of mathematics education [8].

Moreover, there are reports of difficulties in retaining information and basic concepts after the initial teaching phase is evident among students. Thus, there is a need for interventions to improve cognitive retention [9]. In addition, reports show that students have difficulties in understanding content areas in statistics and probability. Based on the findings, there is a deficiency of students in

retention of skills before instruction. Thus, this should be addressed to avoid low performance in upcoming assessments on the subjects. Furthermore, the root cause of misconceptions is the retention of skills learned during instruction [10]. Studies such as Bachelor, Vaughan, and Wall [11], Tintle, Topliff, VanderStoep, Holmes and Swanson [12], and Guvercin, Cilavdaroglu, and Savas [13], and Hamalia and Hamanenga [14] assessed the effects of an intervention on mathematics achievement and retention and the results showed that their intervention showed a positive effect on students' retention. Ajai and Imoko [15] studied if there is a difference in mathematics effect on achievement and retention when grouped according to gender.

Furthermore, the covid-19 pandemic brought unprecedented challenges to education including the shift from face-to-face to distance learning. The covid-19 pandemic stopped face-to-face education to stop the virus from spreading. The Department of Education through the 2020 Education (DepEd) Order No. 12 recommended different learning methods, including online Hybrid, modular, and TV/radio methods [16]. One significant element to consider in the teaching-learning process is how the material is taught because teachers are not used to teaching and learning via online modalities. Students and teachers are significantly impacted [17].

Considering the crucial role of statistics and probability in mathematics education and the impact of retention on the students' performance, this study aimed to determine the retention of the Grade 12 students in Statistics and Probability during Covid-19. Moreover, comparison between and among the retention in each of the topics in Statistics and Probability was also explored to determine what topics need to be emphasized in teaching this subject.

2. Methods

The study used a quantitative approach, particularly descriptive design. The study was conducted at Nueva Vizcaya, General Comprehensive High School (NVGCHS), one of the largest public high school in Nueva Vizcaya, Philippines. Grade 12 students who studied statistics and probability in their eleventh grade were the respondents of the study. There were only twenty (20) STEM students who willingly responded and answered the retention tests. This is one of the limitations of covid-19 especially since the test was given online. The questionnaire for identifying the retention of students towards statistics and probability was validated by four experts. Validator 1 has a doctorate degree, is the Program Chair of the College of Arts and Science Graduate Program of a public state university with 22 years of teaching experience. Validator 2 has a doctorate degree, is Master Teacher I in the Department of Education (DepEd) with 20 years of teaching experience. Validator 3 has a doctorate degree, Teacher III in DepEd with three years of teaching experience. Validator 4 has a doctorate degree, and a faculty at a private university with ten years of teaching experience.

The retention test on statistics and probability was used to measure students' retention. The coverage was Grade 11 statistics and probability topics and corresponding

learning competencies. The topics involved were random variables and probability distribution, normal distribution, sampling and sampling distribution, and estimation parameters. It is a multiple-choice type of test. There were four available choices for students to choose from. In addition, the validity of the researcher-made examination was tested.

The validity results showed that it is valid in terms of clarity and direction of the items (M= 3.25), valid in terms of presentation and organization of items (M=3.25), highly valid for suitability of items (M=3.50), highly valid in terms of its adequateness of the content (M= 3.50), highly valid for the attainment of the purpose of the questionnaire (M= 3.75), highly valid in terms of its objective (M=4.00), and highly valid for scale and evaluation of rating (M=3.50). In general, the questionnaire is highly valid (M=3.54). In terms of its reliability, it has a 0.79 coefficient alpha. This indicates that the reliability test result is acceptable.

The answers of Grade 12 students for the statistics and probability retention test were scored. Every correct response to each item was scored 1 and 0 otherwise. Scores were converted to percent scores to determine the retention rate.

The retention of students in statistics and probability was analyzed and interpreted using Table 1. The DepEd Order No. 8 series of 2015 grading scale with the corresponding descriptor was modified in interpreting the retention rate of the students.

Table 1. Qualitative Scale of the Students' Retention in Statistics and Probability

Percent score	Qualitative Description
90% - 100%	Outstanding Retention Rate
85% - 89%	Very Satisfying Retention Rate
80% - 84%	Satisfying Retention Rate
75% - 79%	Fairly Satisfying Retention Rate
below 75%	Poor Retention Rate

Moreover, frequency counts and percent were used in the tabulation of the summary scores of students in each of the learning competencies of the retention tests. Mean was computed to determine the overall rating of retention of students.

In finding out if significant difference exists between and among the retention of the students in the different topics in Statistics and Probability, preliminary analysis was done to check the assumptions of the tests. The data were checked using one-sample Kolmogorov-Smirnov test because the sample size is less than 30. Table 2 shows the result of one sample Kolmogorov Smirnov test.

Table 2. Test of Normality

Topics	n	Kolmogorov-Smirnov Z	Asymp. Sig. (2-tailed)
Random Variables and Probability Distribution	20	.862	.447
Normal Distribution	20	1.259	.084
Sampling and Sampling Distribution	20	1.061	.210
Estimation of parameters	20	.586	.883

As shown in the table, the p-values of the normality test are beyond 0.05, indicating that the retentions in each topic are normally distributed. Hence, the appropriate test for comparing the retentions was parametric test. The Repeated Measures Analysis of Variance (ANOVA) was performed to answer this problem.

Another assumption of the test is the sphericity. Mauchly's Test of Sphericity was used to check this. Table 3 shows the test for assumption on sphericity.

Table 3. Test of sphericity

Mauchly's Test of Sphericity ^a	Epsilon ^b		
Mauchly's W (5)=.726, p=.340	Greenhouse-Geisser	Huynh-Feldt	Lower-bound
	.815	.944	.333

The assumption of sphericity was violated, as assessed by Mauchly's Test of Sphericity, $p = .340$. Therefore, a Huynd-Feldt correction was applied ($\epsilon = 0.944$). Huynd-Feldt correction is recommended if the estimated epsilon (ϵ) is greater than 0.75.

3. Results and Discussions

The retention of students was determined under each of the learning competencies. In every learning competency, frequencies and percent of students who answered the items correctly in the retention tests are presented. Table 4 presents the different learning competencies for the topic of random variables and probability distribution.

As shown in Table 4, the students have poor retention rates in all the competencies in random variables and probability distribution except in finding the possible values of a random variable (fairly satisfying) and interpreting the mean and the variance of a discrete random variable (satisfying).

Figure 1 shows the sample problems for solving probabilities corresponding to a given random variable. In this item, the retention rate of students was poor.

As shown in Figure 2, the item is about solving probabilities corresponding to a given random variable.

For this item, 70% of students answered A; 10% answered B; 15% answered C; and 5% answered D. The correct answer for this item is letter B, the probability that students will borrow at least two books means borrowing exactly two books or more than two books. This shows that only 10% of the students got the item correctly. Most of the students answered letter A (incorrect answer), which just corresponds to the probability that the students will borrow exactly two books.

Meanwhile, Figure 2 shows the item question wherein the students find for the possible values of a random variable that is fairly satisfying. For this item, students have fairly satisfying retention rate.

Table 4. Retention Rate of Students for the Random Variables and Probability Distribution

Learning Competencies	f	Percent (%)	Qualitative Description (Retention Rate)
Illustrates a random variable (discrete and continuous).	9	45%	Poor
Distinguishes between a discrete and a continuous random variable.	9	45%	Poor
Finds the possible values of a random variable.	15	75%	fairly satisfying
Illustrates a probability distribution for a discrete random variable and its properties.	12	60%	Poor
	14	70%	Poor
Constructs the probability mass function of a discrete random variable and its corresponding histogram.	10	50%	Poor
Computes probabilities corresponding to a given random variable.	2	10%	Poor
Illustrates the mean and variance of a discrete random variable.	11	55%	Poor
Calculates the mean and the variance of a discrete random variable.	9	45%	Poor
	12	60%	Poor
Interprets the mean and the variance of a discrete random variable.	16	80%	Satisfying
Solves problems involving mean and variance of probability distributions.	5	25%	Poor

The School Library records the number of books borrowed by each student in one day, with the following results:

X	0	1	2	3
P(X)	0.20	0.55	0.14	0.11

7. What is the probability that a student will borrow at least 2 books?

- 0.14
- 0.25
- 0.89
- 0.69

Figure 1. Test question to compute probabilities corresponding to a given random variable

3. Given that a random variable x has values $X = \{0,1,2,3,4\}$. What are the possible values of variable x ?

- Value of x could never be 0,1,2,3, or 4 randomly.
- Value of x could be 0,1,2,3, or 4 randomly.
- Value of x could be 0,1, or 2 randomly.
- Value of x could be 3 or 4 randomly.

Figure 2. Test question to find the possible values of a random variable

11. Suppose that the mean of a probability distribution of number of cellphone sold per day is 14. What does this mean?
- This implies that the average number of cellphones sold per day is 14.
 - This implies that the average number of cellphone buyers per day is 14.
 - This implies that there are 14 cellphones sold per day.
 - This implies that there is 14 days average of selling cellphones.

Figure 3. Tests question to interpret the mean and the variance of a discrete random variable

13. Which of the following is **NOT** a property of a standard normal distribution?
- The area under the normal curve bounded by the horizontal axis is 1.
 - The tails of the normal curve are asymptotic to the horizontal axis.
 - The mean, median and mode are at the center.
 - The mean $\mu = 1$ with population standard deviation $\sigma = 0$

Figure 4. Tests question to illustrate a normal random variable its characteristics

16. What is the z-score that corresponds to a score of 63.5 with $\mu = 59$ and $\sigma = 3.5$.
- The z-value that corresponds to the raw score of 63.5 is 1.92.
 - The z-value that corresponds to the raw score of 63.5 is -1.29.
 - The z-value that corresponds to the raw score of 63.5 is -1.92.
 - The z-value that corresponds to the raw score of 63.5 is 1.29.

Figure 5. Test question to convert a normal random variable to a standard normal variable and vice versa.

22. Consider a population consisting of 4,5,3,2,14,18 and 20. From this population, a sample of 4 is to be drawn. Determine whether it is a sampling distribution with known or unknown population variance. Identify the formula to be used when computing the standard error of the mean.
- It is a sampling distribution with unknown variance. The formula for computing the standard error of the mean is $\frac{\sigma}{\sqrt{n}}$.
 - It is a sampling distribution with known variance. The formula for computing the standard error of the mean is $\frac{\sigma}{\sqrt{n}}$.
 - It is a sampling distribution with unknown variance. The formula for computing the standard error of the mean is $\frac{s}{\sqrt{n}}$.
 - It is a sampling distribution with known variance. The formula for computing the standard error of the mean is $\frac{s}{\sqrt{n}}$.

Figure 6. Test question to define the sampling distribution of the sample mean for the normal population when the variance is known and unknown

18. Risa conducted a research of students' life satisfaction in a university. In the process, she just surveyed those she knows. Did she use random sampling?
- Yes, because all the students she knows were surveyed.
 - Yes, because she selected the respondents randomly.
 - No, because only those she knows were selected as respondents.
 - None of the above.

Figure 7. Test question to illustrate random sampling

46. What is the appropriate sample size to estimate the average weight of newborn babies, given that the margin of error is 3.46 and $\sigma = 8.30$ at a 99% level of confidence?
- 38
 - 30
 - less than 30
 - less than 38

Figure 8. Test question to compute for an appropriate sample size using the length of the confidence interval.

Figure 3 shows the corresponding item for finding the possible values of a random variable. For this item, 15% of students answered A; 75% of students answered B; 10% answered C; and no student answered D. The correct answer for this item is letter B, the possible values of the random variable could be 0,1,2, 3, or 4. Majority of students got the correct answer. This indicates that the majority of students can find the possible values of the given random variable.

In addition, the students have satisfying retention rates for interpreting the mean and variance of a random variable. Figure 3 shows the sample item for this learning competency.

Figure 3 shows the corresponding item for interpreting the mean and the variance of a discrete random variable. For this item, 80% of students answered A; 5% answered B; 10% answered C; and 5% answered D. If the mean of the probability distribution for the number of cellphones sold per day is 14, this implies that the average number of sold per day is 14. Majority (80%) of the students got the item correct.

Table 5 presents the different learning competencies for the topic on normal distribution. The frequencies, percent, and qualitative description for retention rates of students are displayed.

As shown in Table 5, the students got poor retention rates for all the learning competencies for normal distribution.

Figure 4 shows the corresponding item for illustrating a normal random variable and its characteristics. For this competency, the students have a poor retention rate.

Figure 4 displays the item to illustrate a normal random variable and its characteristics. Students were to choose which of the given choices is not a property of a standard normal distribution. For this item, 15% of students answered A; 30% of students answered B; 35% of students answered C; and 20% of the students answered D. 20% of students got the correct answer which is letter D, the mean is 1 and population standard deviation of 0. The property of a standard normal table is with a mean of 0 and a population standard deviation of 1. All the other choices are the true property of a standard normal table.

Table 5. Retention Rate of Students for the Normal Distribution

Learning Competencies	f	Percent (%)	Qualitative Description (Retention Rate)
Illustrates a normal random variable and its characteristics.	4	20%	Poor
Constructs a normal curve.	14	70%	Poor
Identifies regions under the normal curve corresponding to different standard normal values.	11	55%	Poor
Converts a normal random variable to a standard normal variable and vice versa.	14	70%	Poor
Computes probabilities and percentiles using the standard normal table.	6	30%	Poor

Meanwhile, Figure 5 shows one of the items wherein 70% of the students got the correct answer, one of the highest percent of students getting the correct answer about normal distribution but still considered as having a poor retention rate.

As shown in Figure 5, the item measures student's understanding of converting a normal random variable to a standard normal variable. Students were to use a formula to convert the given raw to get its z-value. For this item, 5% of students answered A; 10% of students answered B; 15% of students answered C; and 70% of students answered D. Majority (70%) of students know how to convert a normal random variable to a standard normal variable.

For the third topic covered in this study, Table 6 indicates the retention rate of students on the sampling and sampling distribution of the sample mean. The frequencies, percent, and qualitative descriptions for retention rates of students are displayed.

Table 6. Retention Rate of Students for Sampling and Sampling Distribution

Learning Competencies	f	Percent (%)	Qualitative Description (Retention Rate)
Illustrates random sampling.	17	85%	very satisfying
Distinguishes between parameter and statistic.	11	55%	Poor
Identifies sampling distributions of statistics (sample mean).	5	25%	Poor
Finds the mean and variance of the sampling distribution of the sample mean.	5	25%	Poor
Defines the sampling distribution of the sample mean for normal population when the variance is known and unknown.	4	20%	Poor
Illustrates the central limit theorem.	5	25%	Poor
Defines the sampling distribution of the sample mean using the central limit theorem.	6	30%	Poor
Solves problems involving sampling distributions of the sample mean.	6	30%	Poor

As shown in Table 6, students have a poor retention rate in all the learning competencies under-sampling distribution of the sample mean except in illustrating random sampling.

Figure 6 shows the corresponding item for illustrating a normal random variable and its characteristics. For this competency, the students have poor retention rate.

As shown in Figure 6, the item measures students understanding of defining the sampling distribution of the sample mean for a normal population when the variance is known and unknown. Given the specific given and situation, students were to determine if the sampling distribution is with known or unknown population variance, and based on this, they were to identify the formula to be used for the computation of the standard error. For this item, 40% of students answered A; 20% of students answered B; 25% of students answered C; and 15% of students answered D. Most of the students (20%) got the item correctly. This means that some have identified that in the given population of the given problem, the mean and variance of the sampling distribution can be computed, while most students (40%) considered the distribution to have unknown variance.

On the other hand, students have a very satisfying rate of illustrating a random sampling. Eighty-five percent (85%) of students got the corresponding item correctly.

Figure 7 shows the corresponding item for illustrating a random sampling.

Table 7. Retention Rate of Students for Estimation of Parameters

Learning Competencies	f	Percent (%)	Qualitative Description (Retention Rate)
Illustrates point and interval estimations.	9	45%	Poor
Distinguishes between point and interval estimation.	15	75%	fairly satisfying
Identifies point estimator for the population mean.	14	70%	Poor
	13	65%	Poor
Computes for the point estimate of the population mean.	14	70%	Poor
Identifies the appropriate form of the confidence interval estimator for the population mean when: the population variance is known, the population variance is unknown, and the central limit theorem is to be used.	5	25%	Poor
Illustrates the t-distribution.	9	45%	Poor
Identifies regions under the t-distribution corresponding to different t-values.	7	35%	Poor
Identifies percentiles using the t-table.	5	25%	Poor
Computes for the confidence interval estimate based on the appropriate form of the estimator for the population mean.	7	35%	Poor
Solves problems involving confidence interval estimation of the population mean.	5	25%	Poor
Draws conclusion about the population mean based on its confidence interval estimate.	10	50%	Poor
Identifies point estimator for the population proportion.	14	70%	Poor
Computes for the point estimate of the population proportion.	10	50%	Poor
Identifies the appropriate form of the confidence interval estimator for the population proportion based on the central limit theorem.	10	50%	Poor
Computes for the confidence interval estimate of the population proportion.	6	30%	Poor
Solves problems involving confidence interval estimation of the population proportion.	12	60%	Poor
Draws conclusion about the population proportion based on its confidence interval estimate.	12	60%	Poor
Identifies the length of a confidence interval.	12	60%	Poor
Computes for the length of the confidence interval.	7	35%	Poor
Computes for an appropriate sample size using the length of the interval.	3	15%	Poor
Solves problems involving sample size determination.	9	45%	Poor

As shown in Figure 7, the item measures students understanding of illustrating random sampling. Students were asked if random sampling was used given the scenario. For this item, 10% of students answered A; 5% of students answered B; 85% of students answered C; and no student answered D. Majority of the students (85%) got the item correctly. This indicates that majority of students can illustrate or identify if the given scenario used random sampling or not.

As shown in Table 7, the students have poor retention in almost all except one of the learning competencies under estimation of parameters, *illustrates point and interval estimations*.

Figure 8 shows the corresponding item for computing an appropriate sample size using the length of the interval. For this item, students have poor retention rates. This is also the item having the lowest percent (15%) of students getting the correct answer for estimation of parameters. For this competency, the students have a poor retention rate.

As shown in Figure 8, the item measures students' understanding of computing for an appropriate sample size using the length of the interval. Students are asked to find the appropriate sample size to estimate the average weight of newborn babies. For them to answer the item correctly, they also must apply the formula for getting the appropriate sample size. For this item, 15% of students answered A; 45% of students answered B; 30% of students answered C; and lastly 10% of students answered D. Fifteen percent (15%) of students got the item correctly. This means that few students can identify the appropriate sample size.

Only one of the learning competencies under estimation of parameters have a fairly satisfying rate. Seventy-five percent (75%) of students got the correct answer for distinguishing between point and interval estimation. Figure 9 shows the corresponding item for this competency in the retention tests.

As shown in Figure 10, the item measures the understanding of students about point and interval estimates. Students were asked to determine if the identified statements are true about point and interval estimates. For this item, 20% of students answered A; 75% of students answered B; 5% of students answered C; and no student answered D. Seventy-five percent (75%) of the students answered the item correctly. This means that majority of the students have distinguished the difference between point and interval estimate.

In general, students have poor retention rate in majority of the learning competencies for topics about random variables and probability distribution, normal distribution, sampling and sampling distribution, and estimation of parameters. On the other hand, students have a fairly satisfying rate of finding the possible values of a random variable and distinguishing between point and interval estimates. They have a satisfying rate in interpreting the mean and the variance of a discrete random variable. Moreover, they have a very satisfying rate for illustrating random sampling. The findings are similar to Guvercin, et.al [13] who found lower retention of the students regardless of the intervention such as the traditional method. Bachelor, Vaughan, and Wall [11] revealed that students reported issues with retaining information. In particular, teachers stated that students could not recall information and remember essential concepts. Curriculum review indicated that there is a need to do an intervention to improve cognitive retention. Hamalia and Hamanenga [14] justified that there is a learning difficulty shown by students leading to poor performance in probability and mathematics. This led to the use of a discovery learning approach to find out if it can influence students' achievement and retention in probability. Rosli, Capraro, and Capraro [18] assessed the effects of problem posing

intervention on 9th-grade students' mathematics achievement and retention. They found a favorable result in retention in mathematics after using the problem-posing method in teaching the topic of triangles. Similarly, Tintle, Topliff, VanderStoep, Holmes, and Swanson [12] found a higher level of retention among introductory statistics students. Hamalia and Hamanenga [14] found a statistically significant increase in achievement scores and retention scores in probability when the discovery learning

approach was used. Bachelor, Vaughan, and Wall [11] found a positive change in cognitive retention after using a variety of active learning techniques which were student-centered. This shows that teachers need to do something that will help the students improve their retention rate. Moreover, teachers must also consider possible factors affecting the students in solving mathematical tasks such as their attitudes, time limit, beliefs and learning style, and using metacognitive strategy knowledge [19].

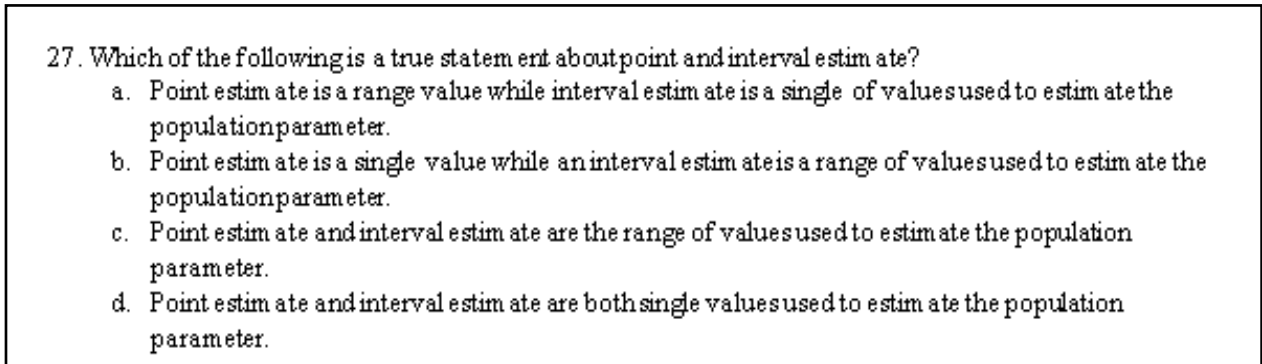


Figure 9. Test question to distinguish between point and interval estimate

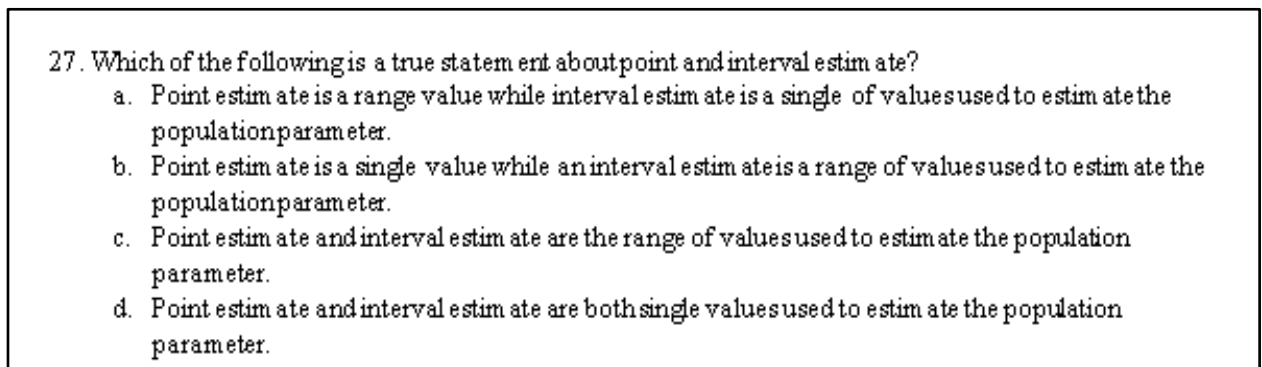


Figure 10. Test question to distinguish between point and interval estimate

Table 8 displays the repeated measures ANOVA result.

As gleaned on the table, the mean scores reveals that the retention of the students in random variable and probably distribution was the highest (m=51.67, s=23.195), followed by normal distribution (m=49.00, s=32.751), estimation of parameters (m=47.27, s=14.554) and the lowest was sampling and sampling distribution (m=36.88, s=19.649). The retention of the students in each of the topics were below 75% indicating that the students have poor retention rate in all the topics. This was also confirmed by the Huynh-Feldt result showing that the retention in each of the topics in Statistics and Probability was not statistically significant, $F(2.832)=2.171, p=.106$. Hence, the retentions of the students in the topics of Statistics and Probability are the same. Generally, all of these topics must be given emphasis in teaching this subject.

4. Conclusions

The students' overall retention in statistics and probability is described as poor retention rate. The learning competencies that had good retention results were

finding the possible values of a random variable, distinguishing point, and interval estimate, interpreting the mean and the variance of a discrete random variable, and illustrating random sampling. However, generally, the retention of the students in each topic of Statistics and Probability is poor. In the related studies, interventions were recommended and employed by the teachers to improve the achievement or retention of the students such as problem-posing and student-centered active learning techniques. In designing an intervention, possible factors that influence students in doing mathematical tasks must also be considered.

Table 8. Significant difference across the Topics of Statistics and Probability

Topic	Mean	s	Test Statistic
Random Variables and Probability Distribution	51.67	23.195	Huynh-Feldt: $F(2.832)=2.171,$ $p=.106$
Normal Distribution	49.00	32.751	
Sampling and Sampling Distribution	36.88	19.649	
Estimation of parameters	47.27	14.554	

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