# For True Conditionalizers Weisberg's Paradox is a False Alarm

Franz Huber
Department of Philosophy
University of Toronto
franz.huber@utoronto.ca
http://huber.blogs.chass.utoronto.ca/

## Contents

**Abstract**

Weisberg (2009) introduces a phenomenon he terms *perceptual undermining*. He argues that it poses a problem for Jeffrey conditionalization (Jeffrey 1983), and Bayesian epistemology in general. This is *Weisberg's paradox*. Weisberg (2014) argues that perceptual undermining also poses a problem for ranking theory (Spohn 2012) and for Dempster-Shafer theory (Shafer 1976). In this paper I argue that perceptual undermining does not pose a problem for any of these theories: for true conditionalizers Weisberg's paradox is a false alarm.

# 1 Weisberg's Paradox

*Weisberg's paradox* consists in the inconsistency of four seemingly plausible constraints. It arises from the following example. Let $D$ be the proposition that the sock really is red, and let $F$ be the hypothesis that the lighting makes all socks look red. At time $t_0$ Sophia does not believe that the sock really is red and has a low degree of belief in $D$. Between $t_0$ and time $t_1$ she has a visual experience by looking at the sock. This visual experience between $t_0$ and $t_1$ causes her, among other things, to form the belief that the sock really is red at $t_1$; it leads to an increase in her degree of belief in $D$ at $t_1$. At time $t_2$ she becomes certain that the lighting makes all socks look red; she assigns a maximal degree of belief to $F$ at $t_2$. Since $F$ is supposed to undermine the visual experience she has had between $t_0$ and $t_1$, this should make her drop her newly acquired belief that the sock really is red at $t_2$ again, and lower her degree of belief in $D$ at $t_2$ back to what it was at $t_0$.

In a probabilistic setting this story is claimed to give rise to the following three constraints:

0. At time $t_0$ Sophia's degree of belief in $D$ is low, say $\Pr_0(D) = .1$.

1a. At time $t_1$ Sophia's degree of belief in $D$ is high, say $\Pr_1(D) = .9$.

2. At time $t_2$ Sophia's degree of belief in $D$ is low again, $\Pr_2(D) = \Pr_1(D \mid F) = Pr_0(D) = .1$.

Sophia's degree of belief function at time $t_2$, $\Pr_2$, comes from her degree of belief function at time $t_1$, $\Pr_1$, by an application of strict conditionalization to the hypothesis $F$. Strict conditionalization is the following update rule:

**Update Rule 1 (Strict Conditionalization)** *If* $\Pr_0(\cdot) : \mathcal{A} \to \mathbb{R}$ *is the ideal doxastic agent's probability measure at time* $t_0$*, and between* $t_0$ *and* $t_1$ *she becomes certain of the proposition* $E \in \mathcal{A}$*,* $\Pr_0(E) > 0$*, in the sense that* $\Pr_1(E) = 1$*, and she does not become certain of any logically stronger proposition (and her probabilities are not directly affected in any other way such as forgetting etc.), then her probability measure at time* $t_1$ *should be* $\Pr_1(\cdot) : \mathcal{A} \to \mathbb{R}$*,*

$$\Pr_1(\cdot) = \Pr_E(\cdot) = \Pr_0(\cdot \mid E) = \Pr_0(\cdot \cap E) / \Pr_0(E).$$

It is important to note that $E$ is assumed to be the *total* evidence the ideal doxastic agent receives between time $t_0$ and time $t_1$.

Sophia's degree of belief function at time $t_1$, $\mathrm{Pr}_1$, is assumed to come from her degree of belief function at time $t_0$, $\mathrm{Pr}_0$, by an application of Jeffrey conditionalization to the evidential partition $\{D, \overline{D}\}$ with input parameters $\mathrm{Pr}_1(D) = .9$ and $\mathrm{Pr}_1(\overline{D}) = .1$. This assumption will turn out to be crucial. Hence it is stated as an independent constraint:

1b. Sophia's degree of belief function at time $t_1$, $\mathrm{Pr}_1$, comes from her degree of belief function at time $t_0$, $\mathrm{Pr}_0$, by an application of Jeffrey conditionalization to the evidential partition $\{D, \overline{D}\}$ with input parameters $\mathrm{Pr}_1(D) = .9$ and $\mathrm{Pr}_1(\overline{D}) = .1$.

Jeffrey conditionalization is the following update rule:

**Update Rule 2 (Jeffrey Conditionalization, Jeffrey 1983)** *If* $\mathrm{Pr}_0(\cdot) : \mathcal{A} \to \mathbb{R}$ *is the ideal doxastic agent's probability measure at time* $t_0$, *and between* $t_0$ *and* $t_1$ *her probabilities on the evidential partition* $\{E_i \in \mathcal{A} : i \in I\}$ *directly change to* $p_i \in \mathbb{R}$, *where* $\sum_{i \in I} p_i = 1$, *and* $p_i = 0$ *if* $\mathrm{Pr}(E_i) = 0$, *and her positive probabilities do not directly change on any finer partition (and her probabilities are not directly affected in any other way such as forgetting etc.), then her probability measure at time* $t_1$ *should be* $\mathrm{Pr}_1(\cdot) : \mathcal{A} \to \mathbb{R}$,

$$\mathrm{Pr}_1(\cdot) = \mathrm{Pr}_{E_i \to p_i}(\cdot) = \sum_{i \in I} \mathrm{Pr}_0(\cdot \mid E_i) \cdot p_i.$$

It is important to note that the evidential partition $\{E_i \in \mathcal{A} : i \in I\}$ and the input parameters $p_i \in \mathbb{R}$ are assumed to be a *complete* description of all doxastically relevant events that happen between $t_0$ and $t_1$. In our example it is important to note that constraint (1b) amounts to the assumption that the only doxastically relevant effect of the visual experience between $t_0$ and $t_1$ is that Sophia's degrees of belief in $D$ and $\overline{D}$ change to $\mathrm{Pr}_1(D) = .9$ and $\mathrm{Pr}_1(\overline{D}) = .1$. In particular, it follows from constraint (1b) that $F$ is not directly affected, in any doxastically relevant way, by Sophia's visual experience between $t_0$ and $t_1$. Among other things, this means that, at $t_1$, Sophia does not also form a belief about how she came to be more confident in $D$ (or, if she has a belief at $t_1$ about how she came to be more confident in $D$, then it is the same belief that she had at $t_0$, *before* she had the visual experience). In order to simplify matters, let us assume, as is reasonable, that, at $t_0$, Sophia has no particular belief about what will happen between $t_0$ and $t_1$. Then constraint (1b) implies that, at $t_1$, Sophia remains agnostic as to whether it was by vision, or by some other form of perception, or by testimony, or by clairvoyance that she became more confident in $D$.

In other words, unless she already does so at $t_0$, Sophia does not believe at $t_1$ that the experience she undergoes between $t_0$ and $t_1$ is a *visual* experience. For all she believes at $t_1$, the experience she undergoes between $t_0$ and $t_1$ may not even be a *perceptual* experience. Indeed, given our reasonable assumption, for all she believes at $t_1$, what happens between $t_0$ and $t_1$ may not even be an *experience* of hers. *We* know this from the way the story was told, but, according to constraint (1b), *she* does not.[1]

So far, so good. Now the allegedly bad news. Jeffrey conditionalization is *rigid*. This implies that Jeffrey conditionalization preserves probabilistic independence of the members of the evidential partition. If a proposition $A$ is independent of the evidential proposition $D$ according to Sophia's degree of belief function at time $t_0$, $\mathrm{Pr}_0(A \mid D) = \mathrm{Pr}_0(A)$, then $A$ is also independent of $D$ according to her degree of belief function at a time $t_1$, $\mathrm{Pr}_1(A \mid D) = \mathrm{Pr}_1(A)$.

Weisberg (2009; 2014) thinks that this poses a problem for Jeffrey conditionalization, and Bayesian epistemology in general. He does so, because there is the following fourth constraint:

3. $F$ is independent of $D$ according to Sophia's degree of belief function at time $t_0$, $\mathrm{Pr}_0(F \mid D) = \mathrm{Pr}_0(F)$.

Weisberg (2009; 2014) is, of course, free to stipulate any constraints he wants. However, in order to evaluate the joint plausibility of his constraints, we need to understand what this condition says, and what it does not say. The condition says: at $t_0$, the degree to which Sophia believes that the lighting makes all socks look red has no bearing on the degree to which she believes that the sock really is red. The condition does *not* say: at $t_0$, whether or not the lighting makes all socks look red has no bearing on whether or not the sock really is red.

Together with the rigidity of Jeffrey conditionalization this fourth constraint implies that $F$ is independent of $D$ according to Sophia's degree of belief function at time $t_1$, $\mathrm{Pr}_1(F \mid D) = \mathrm{Pr}_1(F)$. However, if $F$ is independent of $D$ according to Sophia's degree of belief function at time $t_1$, $\mathrm{Pr}_1(F \mid D) = \mathrm{Pr}_1(F)$, then $D$ is independent of $F$ according to her degree of belief function at time $t_1$, $\mathrm{Pr}_1(D \mid F) = \mathrm{Pr}_1(D)$. In this case her degree of belief in $D$ at time $t_2$ equals her degree of belief in $D$ at time $t_1$, $\mathrm{Pr}_2(D) = \mathrm{Pr}_1(D) = .9$. This contradicts the third constraint according to which $\mathrm{Pr}_2(D) = .1$.

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[1] If, contrary to what constraint (1b) implies, Sophia had even the slightest of hunches about what might have caused the changes in her degrees of belief in $D$ and in $\overline{D}$, the evidential partition would include other propositions besides $D$ and $\overline{D}$. In this case Weisberg's paradox would not arise.

Weisberg's paradox consists in this inconsistency. In the next section I will defend Jeffrey conditionalization and argue that Weisberg's paradox is resolved once we notice the implications of constraints (0-1) and (3) – in particular, (1b) – which make constraint (2) utterly implausible.

## 2   Jeffrey Conditionalization Defended

Weisberg's paradox consists in the inconsistency of the four seemingly plausible constraints (0-3), where Jeffrey conditionalization is part of constraint (1). For Weisberg (2009; 2014) the culprit is constraint (1) with Jeffrey conditionalization. I want to defend Jeffrey conditionalization.

Constraints (0-1) imply that what Sophia has experienced between $t_0$ and $t_1$ when looking at the sock results in an increase in her degree of belief in the proposition $D$ that the sock really is red: $\Pr_1(D) > \Pr_0(D)$. However, in conjunction with the allegedly plausible constraint (3) constraints (0-1) also imply that what Sophia has experienced between $t_0$ and $t_1$ makes her hold onto her degree of belief in the hypothesis $F$ that the lighting makes all socks look red: $\Pr_1(F) = \Pr_0(F)$. I want to use this consequence of constraints (0-1) and (3) to motivate my defense of Jeffrey conditionalization.

Roughly speaking, the former inequality $\Pr_1(D) > \Pr_0(D)$ says that at $t_1$ Sophia thinks that what she has experienced between $t_0$ and $t_1$ – or better, as Sophia may not even believe that it was an experience: what has happened between $t_0$ and $t_1$ – is related to $D$. The difference between $\Pr_1(D)$ and $\Pr_0(D)$, in whichever way it is measured, reflects how likely she thinks, at $t_1$, that what has happened between $t_0$ and $t_1$ is related to $D$. The latter equation $\Pr_1(F) = \Pr_0(F)$ says, roughly, that at $t_1$ she thinks that what has happened between $t_0$ and $t_1$ has nothing to do with $F$. The difference between $\Pr_1(F)$ and $\Pr_0(F)$, in whichever way it is measured, is nil, and that is how likely she thinks it, at $t_1$, that what has happened between $t_0$ and $t_1$ is related to $F$. In particular, this latter equation says, roughly, that, at $t_1$, Sophia thinks that $F$ is not a potential underminer for what has happened between $t_0$ and $t_1$.

Less roughly speaking, on the one hand constraints (0-1) say that Sophia's belief in $D$ is directly affected by what happens between $t_0$ and $t_1$ in such a way that she ends up being more confident in $D$ at $t_1$ than she was at $t_0$. On the other hand constraints (0-1) say that Sophia's belief in $F$ is *not* directly affected by what happens between $t_0$ and $t_1$. Constraints (0-1) and the allegedly plausible stipulation (3) add to this that Sophia's belief in $F$ is not indirectly affected by what happens between $t_0$ and $t_1$ either. Together constraints (0-1) and (3) thus say that Sophia's belief in $F$ is neither directly nor indirectly affected by what happens between $t_0$ and $t_1$. In particular, constraints (0-1) and (3) say that, at $t_1$, Sophia thinks that $F$ is not a potential underminer for what has happened between $t_0$ and $t_1$.[2]

In other words, constraints (0-1) and (3) imply that at $t_1$ Sophia thinks that what has happened between $t_0$ and $t_1$ may be due the fact that the sock really is red, $D$, but is definitely not due to the fact that the lighting makes all socks look red, $F$. Given this consequence of constraints (0-1) and (3), constraint (2) clearly should be rejected: constraint (2) says that, at $t_1$, Sophia thinks that $F$ is a potential underminer for what has happened between $t_0$ and $t_1$, whereas it follows from constraints (0-1) and (3) that, at $t_1$, she thinks that $F$ is not a potential underminer for what has happened between $t_0$ and $t_1$.

Here is a different way of putting things. Suppose we modeled the change of Sophia's degree of belief function from $t_0$ to $t_1$ by an application of strict conditionalization to the appearance proposition $D^*$ that the sock appears to be red, $\Pr_1(\cdot) = \Pr_0(\cdot \mid D^*)$. In this case Sophia would believe that the actual color of the sock is relevant to the apparent color of the sock, $\Pr_1(D) = \Pr_0(D \mid D^*) > \Pr_0(D)$. More importantly, however, she would presumably also believe that the apparent color of the sock is relevant to the hypothesis that the lighting makes all socks look red, $\Pr_1(F) = \Pr_0(F \mid D^*) > \Pr_0(F)$. Consequently we would not have the consequence $\Pr_1(F) = \Pr_0(F \mid D^*) = \Pr_0(F)$.

Now in Weisberg's example there is no appearance proposition $D^*$ that Sophia becomes certain of between $t_0$ and $t_1$. Instead of an application of strict conditionalization to the appearance proposition $D^*$ we have an application of Jeffrey conditionalization to the evidential partition $\{D, \overline{D}\}$ that is caused by some visual experience $d^*$. Instead of the appearance proposition $D^*$ that Sophia becomes certain of, the doxastically relevant effects of the visual experience $d^*$ are now described more indirectly: they correspond to the differences between Sophia's degrees of belief in $D$ and $\overline{D}$ at $t_0$ and her degrees of belief in $D$ and $\overline{D}$ at $t_1$. The visual experience $d^*$ is non-propositional evidence that is reflected in the different shapes of Sophia's two degree of belief functions at $t_0$ and at $t_1$ on the evidential partition $\{D, \overline{D}\}$. Most importantly, in contrast to the above case where Sophia becomes certain of an *appearance* proposition, and thus learns something about what drives the change in her degrees of belief, constraint (1b) *ex*cludes informa-

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[2]The conjunction of constraints (0-1) and (3) is logically strictly stronger than its consequence $\Pr_0(F) = \Pr_1(F)$. The latter equation can be true if constraints (0-1) or (3) are false, because the various effects on Sophia's belief in $F$ may "cancel out." For instance, what happens between $t_0$ and $t_1$ may affect Sophia's belief in the four propositions $X \cap F, X \cap \overline{F}, \overline{X} \cap F, \overline{X} \cap \overline{F}$, for some proposition $X$, even though Sophia's degrees of belief in $X \cap F$ and $\overline{X} \cap F$ may sum to the same number at $t_0$ and at $t_1$. It is the conjunction of constraints (0-1) and (3), not its consequence, that says that, at $t_1$, Sophia thinks that $F$ is not a potential underminer for what has happened between $t_0$ and $t_1$.

tion about what drives the change in Sophia's degrees of belief in $D$ and $\overline{D}$. For all Sophia believes, the change in her degrees of belief in $D$ and $\overline{D}$ may be due to a lapse of rationality.

Given these consequences it becomes clear that, in the presence of constraints (0-1) and (3) – in particular, constraint (1b) – constraint (2) is utterly implausible. If Sophia does not believe that the change in her degrees of belief in $D$ and $\overline{D}$ between $t_0$ and $t_1$ has been caused by her vision, why should she believe that $F$ can undo this doxastically relevant effect of what has happened between $t_0$ an $t_1$? The way the story is told makes it clear to *us* that it was her vision that caused her increase in confidence in $D$. However, as long as this information is not also made available to *her*[3], there is no reason whatsoever to assume that her becoming certain of $F$ should have any effect at all on her degree of belief in $D$.

To be sure, there are potential underminers $F$ for Sophia's visual experience that takes place between $t_0$ and $t_1$, and constraint (2) can be satisfied. However, if constraint (2) is satisfied for some potential underminer $F$, then this potential underminer $F$ must violate constraint (3) or constraint (1). Constraint (3) is violated by $F$ if $F$ is not independent of $D$ according to $\mathrm{Pr}_0$. Constraint (1) is violated by $F$ if Jeffrey conditionalization is applied to an evidential partition $\{E_i : i \in I\}$ whose members are not all logically independent of the potential underminer $F$, and which must thus be more fine-grained than $\{D, \overline{D}\}$, say, $\{D \cap F, \overline{D} \cap F, D \cap \overline{F}, \overline{D} \cap \overline{F}\}$.

If constraint (3) is violated by $F$, but constraint (1) holds, then $F$ is indirectly affected by the visual experience that takes place between $t_0$ and $t_1$, and Jeffrey conditionalization governs this indirect way of being affected. In this case $F$ figures in the output of Jeffrey conditionalization, which tells Sophia, among other things, what to believe about $F$. If constraint (1) is violated by $F$, then $F$ is directly affected by the visual experience that takes place between $t_0$ and $t_1$, and Jeffrey conditionalization has to be applied to an evidential partition some of whose members are logically dependent on $F$. In this case $F$ figures in the input of Jeffrey conditionalization, and Sophia has to specify her new degrees of belief for all these members, including those that logically depend on $F$, before Jeffrey conditionalization can be applied.

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[3]One way of making this information available to Sophia is by using Shafer (1985)'s notion of a *protocol*. Halpern (2003: ch. 6) uses protocols to solve Freund (1965)'s puzzle. Spohn (2012: sct. 9.3) uses protocols to solve the puzzle of the three prisoners (Mosteller 1965: problem 13) that is also known as the Monty Hall problem. Halpern (ms) uses protocols to solve the Doomsday Argument and the Sleeping Beauty Problem. A different proposal is discussed in the Appendix.

Either way there is no problem for Jeffrey conditionalization. We just have to realize that, while a change of Sophia's degrees of belief from $t_0$ to $t_1$ can be undermined, it can only be undermined by a hypothesis $F$ that is doxastically affected by what drives the former change. This can happen indirectly by $F$ not being probabilistically independent of the members of the evidential partition and thus violating the allegedly plausible stipulation (3). Or it can happen directly by $F$ not being logically independent of all members of the evidential partition to which Jeffrey conditionalization is applied. Which is determined by experience, not by methodology.

For these reasons I conclude that Weisberg's paradox may affect the applicability of Jeffrey conditionalization, but not its validity. Weisberg's paradox does not undermine Jeffrey's rule of conditionalization: for true conditionalizers Weisberg's paradox is a false alarm. Parallel considerations show that perceptual undermining does not pose a problem for ranking theory or Dempster-Shafer theory either.

# 3 Appendix

One way of making the information that it was her vision that caused her increase in confidence in $D$ available to Sophia is by using Shafer (1985)'s notion of a *protocol*. Protocols have proved to be a powerful tool in solving paradoxes. For instance, Halpern (2003: ch. 6) uses protocols to solve Freund (1965)'s puzzle. Spohn (2012: sct. 9.3) uses protocols to solve the puzzle of the three prisoners (Mosteller 1965: problem 13) that is also known as the Monty Hall problem. Halpern (ms) uses protocols to solve the Doomsday Argument and the Sleeping Beauty Problem. It is only natural that protocols can also be used to solve Weisberg's Paradox.

A different proposal for making the information that it was Sophia's vision that caused her increase in confidence in $D$ available to Sophia is presented in Gallow (2014). Gallow (2014) first proposes the following update rule:

**Update Rule 3 (Gallow Conditionalization I, Gallow 2014)** *If* $\Pr_0(\cdot) : \mathcal{A} \to \mathbb{R}$ *is the ideal doxastic agent's probability measure at time $t_0$, and between $t_0$ and $t_1$ she receives total evidence of the form $\{(T_i, E_i) : i \in I\}$, where the $T_i \in \mathcal{A}$ form a partition of the underlying set of possible worlds $W$, and her probabilities are not directly affected in any other way such as forgetting etc., then her probability measure at time $t_1$ should be* $\Pr_1(\cdot) : \mathcal{A} \to \mathbb{R}$,

$$\Pr_1(\cdot) = \sum\nolimits_{i \in I} \Pr_0(\cdot \mid T_i \cap E_i) \cdot \Pr_0(T_i).$$

The interpretation of a pair $(T_i, E_i)$ is that the ideal doxastic agent's evidence is $E_i$, provided $T_i$ is the case. For instance, Sophia's total evidence may be that the sock really is red, provided the lighting does not make all socks look red and everything else is normal as well; and nothing otherwise: $\{(N, E), (\neg N, W)\}$.

Gallow conditionalization I is an instance of Jeffrey conditionalization on the evidential partition $\left\{T_i \cap E_i, T_i \cap \overline{E_i} : i \in I\right\}$ with input parameters $\Pr_1(T_i \cap E_i) = \Pr_0(T_i)$ and $\Pr_1\left(T_i \cap \overline{E_i}\right) = 0$. Unfortunately it does not allow the ideal doxastic agent to ever change her confidence in any of the theories $T_i$, i.e. $\Pr_1(T_i) = \Pr_0(T_i)$.

For this reason Gallow (2014) generalizes his first update rule to the following second update rule:

**Update Rule 4 (Gallow Conditionalization II, Gallow 2014)** *If $\Pr_0(\cdot) : \mathcal{A} \rightarrow \mathbb{R}$ is the ideal doxastic agent's probability measure at time $t_0$, and between $t_0$ and $t_1$ she receives total evidence of the form $\{(T_i, E_i) : i \in I\}$, where the $T_i \in \mathcal{A}$ form a partition of the underlying set of possible worlds $W$, and her probabilities are not directly affected in any other way such as forgetting etc., then her probability measure at time $t_1$ should be $\Pr_1(\cdot) : \mathcal{A} \rightarrow \mathbb{R}$,*

$$\Pr_1(\cdot) = \sum_{i \in I} \Pr_0(\cdot \mid T_i \cap E_i) \cdot \Pr_0(T_i) \cdot \Delta_i,$$

*where $\Delta_i$ is a non-negative real number representing the degree to which the total evidence $\{(T_i, E_i) : i \in I\}$ (dis)confirms theory $T_i$.*

Contrary to what Gallow (2014: 21) claims his second update rule does not generalize Jeffrey conditionalization. Indeed, quite the opposite is the case. Gallow conditionalization II is also just an instance of Jeffrey conditionaliztion on the evidential partition $\left\{ T_i \cap E_i, T_i \cap \overline{E_i} : i \in I \right\}$ with input parameters $\Pr_1(T_i \cap E_i) = \Pr_0(T_i) \cdot \Delta_i$ and $\Pr_1\left(T_i \cap \overline{E_i}\right) = 0$. (As Gallow (2014: 25ff) shows, the sum $\sum_{i \in I} \Pr_0(T_i) \cdot \Delta_i = \sum_{i \in I} \Pr_1(T_i \cap E_i) = \sum_{i \in I} \left( \Pr_1(T_i \cap E_i) + \Pr_1\left(T_i \cap \overline{E_i}\right) \right)$ equals 1, and so the constraints of Jeffrey conditionalization are satisfied.)

# Acknowledgments

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