

Agent-Based Models and Simulations in Economics and Social Sciences: from conceptual exploration to distinct ways of experimenting

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Abstract. Now that complex Agent-Based Models and computer simulations spread over economics and social sciences - as in most sciences of complex systems -, epistemological puzzles (re)emerge. We introduce new epistemological tools so as to show to what precise extent each author is right when he focuses on some empirical, instrumental or conceptual significance of his model or simulation. By distinguishing between models and simulations, between types of models, between types of computer simulations and between types of empiricity, section 2 gives conceptual tools to explain the rationale of the diverse epistemological positions presented in section 1. Finally, we claim that a careful attention to the real multiplicity of *denotational powers of symbols* at stake and then to the *implicit routes of references* operated by models and computer simulations is necessary to determine, in each case, *the proper epistemic status and credibility of a given model and/or simulation*.

Keywords: Agent-Based models, simulation, social sciences, economics, epistemology, conceptual exploration, experiment, iconicity, denotational hierarchy

Introduction: Methodical Observation versus Conceptual Analysis

Models and empirical enquiries have often been opposed. Such an opposition between observational experiment and reasoning has led to classical oppositions: empirical sciences are seen as based on methodic observation (inquiry, experiment) whereas theoretical and modeling approaches are thought as founded on a conceptual or hypothetico-deductive approach.

Amazingly, even if simulation is still often defined with reference to modeling (e.g. as a “dynamical model ... that imitates a process by another process”, [28]), it has been more systematically compared to a kind of experiment or to an

intermediary method between theory and experiment ([40], [50]). In agent-based simulation, Tesfatsion [49] talked about “computational laboratory” as a way “to study complex system behaviors by means of controlled and replicable experiments”, and Axelrod [3] claimed that simulation in social sciences is “a third way for doing science”, between induction and deduction.

The first aim of this paper is to review, discuss and extend these rather converging positions on simulations in the case of agent-based models of simulation in economics and social sciences, based on MAS (multi-agent systems) software technology [10, 11]. In this case, as underlined by Axelrod [3], simulation begins with *model building activity*, even if analytical exploration of the model is often impracticable. Recently, authors have proposed to distinguish between ontology design and model implementation in this initial step of model engineering [7, 32]. As model building is an unavoidable phase of agent-based simulation, the first section is a review of the main epistemologies of models, with a special interest for economics models, taking the paradigmatic Schelling models of segregation as an example. It stresses some recent claims about the empirical nature of models in economics and social sciences. More and more authors say that models and simulations in social sciences - specifically as far as multi-agent models are concerned - present a shift from a kind of “conceptual exploration” to a new way of doing “experiments”. Section two recalls some of the recent puzzles about the real empiricity of such practices. It proposes to adapt and use the two notions of *sub-symbolization* [45] and *denotational hierarchy* [19] to explain further crucial differences, (1) between models and simulations, (2) between models and simulations of models and (3) between kinds of simulations. Those concepts enable to explain why multi-agent modeling and simulation produce new kinds of empiricity, not far from the “epistemic power” of ordinary experiments. They enable to understand why some authors are right to disagree on the epistemic status of models and simulations, especially when they do not agree on the *denotational level* of the systems of symbols they implement.

1. Modeling and experiment

1.1. Epistemological conceptions on scientific models

Since the beginning of the 20th century, the term “model” has spread in the descriptions of scientific practices, particularly in the descriptions of the practices of formalization.

Having founded their first expansion in a movement of emancipation toward monolithic theories in physics (such as mechanics), scientific models have first been explained by epistemologists through systematic comparisons to theories. Consequently, in the first neo-positivist epistemology, models were viewed not as autonomous objects, but as theoretically driven derivative instruments. Following the modelistic turn in mathematical logic, the semantic epistemological conception of scientific models persisted to emphasize on theory. For such a *view*, a model is a structure of objects and relations (more or less abstract) that is one of the *possible*

interpretations of a given theory. But it stresses also the different layers (cleavage) of formal structures.

More recently, models have been compared to experimental practices [12, 13, 16, 26, 39]. For a rather similar pragmatic point of view [38], models are “autonomous mediators” between theories, practices and experimental data. They are built in a singular socio-technical context and in order to solve a specific and explicit problem emerging from this context.

1.2 An open and pragmatic view: the model as a questionable construct

Without going further in the debate between semantic and pragmatic views in epistemology of models, it is possible to get some insight on the weak relations between scientific models and theories through the general and pragmatic characterization of a model by Minsky [36]:

“To an observer B, an object A* is a model of an object A to the extent that B can use A* to answer questions that interest him about A”.

Minsky minimally sees a model as a questionable construct. As a construct, the model is an abstraction of an “object domain” formalized by means of an unambiguous language. Such a characterization assumes that the model A* is *sufficient* to answer the question asked by B (see [2]).

Note that this loose characterization does not imply that the model is based on a relevant theory of the empirical phenomenon of the considered domain. It is enough to say that such a questionable construct exemplifies some definite “constraints on some specific operations” [31]. Therefore, in general, a scientific model is not an interpretation of a pre-existing theory, but a way to explore some properties in the virtual world of the model. In particular, according to Solow [46], it can serve to evaluate the explaining power of some hypothesis (constructed by abduction) isolated by abstraction: “the idea is to focus on one or two causal or conditioning factors, exclude everything else, and hope to understand how just these aspects of reality work and interact” (p. 43). Due to this characteristic, some authors have compared the model to real experiment. Let us precise further some of the points that models share with experiment.

1.3 The “isolative analogy” between models and experiments

Economists distinguish usually the abstract worlds of the models from the “real world” of the empirical phenomenon. This neither means that they are pure formalists nor that talking about a “real world” implies a metaphysical realistic commitment. This is just to underline the recognition of a problematic relationship between the abstract world of the models and the concrete empirical reality.

For Mäki, abstractions in models are similar to abstractions in experiments as they both can be interpreted as a *kind of isolation*. Accordingly, model building can be viewed as a quasi-experimental activity or as the “economist’s laboratory” [33, 34, 35]. This analogy between models and experiments is called “isolative analogy” by Guala [25]. From Mäki’s standpoint, a model can be said to be experimented in its

explanatory dimension: the finality of such a model is to explore the explanatory power of some causal mechanism taken in isolation. Significantly, Guala is less optimistic than Mäki. He refuses to overlook the remaining differences between a model and an experiment:

“In a simulation, one reproduces the behavior of a certain entity or system by means of a mechanism and/or material that is radically different in kind from that of a simulated entity (...) In this sense, *models simulate* whereas *experimental systems do not*. Theoretical models are conceptual entities, whereas experiments are made of the same ‘stuff’ as the target entity they are exploring and aiming at understanding” ([25], p.14).

It is often by using the mediating and rather paradoxical notion of “stylized facts” that authors give themselves the possibility to overlook this difference in “stuff”, when comparing models and experiments.

Sugden [47] suggests a slightly different approach in which two worlds are to be distinguished. The abstract “world of the model” is a way to evaluate through virtual experiments the explanatory power of some empirically selected assumptions. The problematic relationship between this abstract world and the real one can be summarized by two questions. To what extent such a virtual world can have some link with the “real world”? What kind of (weak) realism is at stake here?

1.4. The scope and meaning of Schelling’s conjecture according to Sugden (2002)

A model (in a broad meaning) can be seen as an abstract object. As such, it is based on a principle of parsimony. It is a conceptual simplification which stresses one or more conjecture(s) concerning the empirical reality. Moreover, it is built to answer a specific question which can have an empirical origin. In this specific case, one talks about empirically oriented conceptualization.

Sugden [47] takes Schelling’s model of segregation [44] as an example. According to Solow [45], there is a first empirical question in every process of modeling: a regularity (or “stylized fact”) is previously observed in phenomenological material from empirical reality. In the Schelling case, it is the persistence of racial segregation in housing for the Schelling model of segregation. Then a conjecture is proposed. In this case, Schelling’s conjecture says that this phenomenon (persistent racial segregation in housing) could be explained by a limited set of causal factors (parsimony).

According to this conjecture, a simplified model is constructed where agents interact only locally with their 8 direct neighbors (within a Moore neighborhood). No global representation about the residential structure is available to agents. The only rule specifies that each agent would stay in a neighborhood with up to 62% of people with another color. Finally, the simulation of the model shows that a slight perturbation is sufficient to induce local chain reactions and emergence of segregationist patterns. I.e., “segregation” (clusters) is observed as an emergent property of the model.

This does not mean that these factors are the only possible explaining ones, neither that there are effectively the main causal factors for the empirical observed phenomenon. This empirical observation of the model only gives the right to claim

that these factors are *possible explanatory candidates*. What is tested with this approach is nothing but “conditions of possibilities” and not directly the genuine presence of these conjectured factors in the empirical reality.

In the Schelling case, (1) he observes a regularity R in the phenomenological data observed from the “real world” (here it is that persistent racial segregation in housing); (2) he conjectures that this regularity can be explained by a limited set (parsimony) of causal factors F (here it is the simple local preferences about neighborhood).

Hence, according to Sugden [47], Schelling’s approach relies on three claims:

- (1) R occurs (or often occurs)
- (2) F operates (or often operates)
- (3) F causes R (or tends to cause it)

Schelling doesn’t present explicitly these claims as testable hypotheses. But claims (1) and (2) get informal evidence from selected case studies.

The unresolved question concerning the problematic relationship between the conjectural and abstract “world of the model” and the “real world” remains. Sugden [47] discusses different strategies to answer this question. He rejects first the instrumentalist view [15] which represents models as (testable) instruments with predicting power. For Sugden, the goal of Schelling clearly is an *explanatory one*. Contrary to the instrumentalists’ view, Schelling does not construct “any explicit and testable hypothesis about the real world” ([47], p.118). Sugden discusses also the notions of models as conceptual explorations, thought experiments and explaining metaphors. According to Hausman [29], all these approaches are incomplete, because the persistent gap between the “world of the model” and the “real world” is not filled. Sugden suggests filling the gap by an inductive inference: the *credible world* argument.

In the suggested interpretation, Schelling connects first *in abstracto* real causes (segregationist preferences) to real effects (segregationist cluster emergence). Afterwards, instead of “testing” empirical predictions from the models, he tries to convince us of the credibility of the corresponding assumptions. Schelling’s unrealistic model is “supposed to give support to these claims about real tendencies”. For Sugden, this method “is not instrumentalism: it is some form of realism” ([47], p.118). Before going deeper in this question of “*realist*” *credible world* (sect. 1.6), let us discuss first the strategy of “conceptual exploration”.

1.5. Conceptual exploration and “internal validity”

Following Hausman [29], we speak of the use of a model as a “conceptual exploration” when we put the emphasis on the *internal properties* of the model itself, without taking into account the question of the relationship between the “model world” and the “real world”. The study of the model’s properties is the ultimate aim of this approach. The relevant methods used to explore and evaluate “internally” the properties of the model depend on its type, and not on its relationship with the corresponding empirical phenomenon.

Similarly to a test of consistency performed on a set of concepts put together in a form of a closed verbal argument, the properties of the model which are tested here

are essentially evaluated in terms of *consistency*. From this standpoint, the model is viewed as a pure conceptual construct. As Hausman [29] underlines, conceptual exploration can be valuable because there are numerous examples of unsuspected inconsistencies or unidentified properties in the existing models.

An extension of this method enables an assessment of the *robustness* of the results of the model with respect to variations in its hypotheses (as in the studies of sensibility). But it is important to note that when the exploratory method is no more purely analytic, some scholars claim that it becomes a quasi-experimental activity.

Following Guala [24] on this point, we can interpret all the means used by this approach of conceptual exploration as different efforts to validate the model in the sense of an *internal validity*:

“Whereas internal validity is fundamentally a problem of identifying causal relations, external validity involves an inference to the robustness of a causal relation outside the narrow circumstances in which it was observed and established in the first instance” ([24], p. 1198-1199).

But gradually, when analyses of robustness are more and more adopted and extended, the assessment process can be interpreted much more properly in terms of *external validity*. Guala sees a huge gap between internal and external validity because, for him, models always simulate with the aid of radically different stuffs from the ones of the real world. But many cases of development of conceptual explorations on models show that there is a more gradual and progressive shift from a “conceptual exploration”, strictly speaking, to a first kind of “external validation”. According to us, that is the reason why some scholars persist to use - with some good reasons - the notion of *quasi-experimental activity*. So, let’s go now a bit further with this notion of “credible worlds”.

1.6. Models as “credible worlds” (Sugden, 2002)

In this concern, Sugden’s approach is interesting. First, it gives more details on the nature of the conceptual exploration performed through a model. Second, by introducing the notion of “credible world”, it proposes to treat more directly the link between the model world and the real world.

According to Sugden, economists “formulate credible (*ceteris paribus*) and pragmatically convenient generalizations concerning operations related to the appropriate causal variable”. Then, the model analyst uses deductive reasoning to identify what effects these factors will have under these specific hypotheses (i.e. in this particular isolated environment). These analyses of robustness provide *reasons to believe* that the model is not specific but could be generalized, including the original model as a special case.

To that extent, the corresponding cognitive process is an *inductive inference*, i.e. an inference from the cases of already experimented models to more general model cases. But this mode of reasoning concerns scenarios for conceptual exploration which remain within the world of models. From this viewpoint, the test of robustness cannot really be interpreted as being on the adequacy between the world of models and the real world. As Sugden emphasizes, some special links between the two worlds still are required.

At this point, Sugden introduces the idea that a model has to be thought as a “credible world”. This argument works as an inductive inference too, but *an inference from the model world to the real world*. The desirable outcome is the recognition of some “significant similarity” between these two worlds. For Sugden, Schelling constructed “imaginary cities” which are easily understandable because of their explicit generative mechanisms. “Such cities can be viewed as possible cities, together with real cities”. Through Schelling’s argument, we are invited to make the inductive inference that similar causal processes occur in real cities.

The whole process can be summed up as 3 phases of an abductive process:

(a) The modeler observes that segregation occurs in the real world, and makes the abduction (in a narrow sense) or conjecture that segregation (S) is caused by individual preferences over neighborhood structure (IPoNS).

(b) The modeler experiments and deduces that in the model world, S is caused by IPoNS.

(c) The modeler infers that there are some good reasons to believe that IPoNS also operates in the real world, even if it is not the only possible cause of S.

That is, IPoNS is a credible candidate to explain S and then the “world of model” is a “possible reality” or a “parallel reality”. Sugden [47] specifies this kind of “realism”: “Here, the model is realistic in the same sense as a novel can be called realistic [...] the characters and locations are imaginary, but the author has to convince us that they are credible” (p.131).

Clearly, such an assessment of the “model world” is not strictly about its empirical testability, but more about its argumentative power. Anyway, the notions of “similar causal processes” and “parallel reality” can play a role in an empiricist epistemology of simulation. But Sugden does not give us much precision on these notions of “similarity” and “parallelism”. The notions of “significant similarity” and “constraint on the operations” of Livet [31] also could help us to go further into the evaluation of the empirical roles of models and simulations.

Section 2 aims to introduce conceptual tools (such as *relative iconicity*) so as to enter in more details in what determines the epistemic status of models and computer simulations, hence in what determines their credibility.

2. Models, Simulations and Kinds of Empiricity

First of all, although they seem to remain constantly linked in practice - even in those simulations based on multi-models and multi-formalisms [43] -, it is necessary today to conceptually distinguish models from simulations and to characterize the practice of computer simulation (CS) *apart from a central reference to a unique model*.

2.1. Models and computer simulations: some more definitions and characterizations

Roughly speaking, a model still can be defined as a formal construct possessing a kind of unity, formal homogeneity and simplicity. These unity, simplicity and

homogeneity are chosen so as to satisfy a specific request (prediction, explanation, communication, decision, etc.).

But, concerning simulation, current definitions need now to be modified and somewhat generalized. Scholars, especially in physics and engineering sciences, were often used to say that “a simulation is a model in time”. For instance, according to [28]:

“Simulations are closely related to dynamic models” [i.e. models with assumptions about the time-evolution of the system] ... More concretely, a simulation results when the equations of the underlying dynamic model are solved. This model is designed to imitate the time evolution of a real system. To put it another way, a simulation imitates a process by another process” ([28], p. 82).

Humphreys [30] follows Hartmann [28] on the “dynamic process”. For Parker (forthcoming work quoted by [56]), a simulation is:

“A time-ordered sequence of states that serves as a representation of some other time-ordered sequence of states ; at each point in the former sequence, the simulating system’s having certain properties represents the target system’s having certain properties.”

It is true that a simulation takes time as a step by step operation. It is true too that a modeled system interests us in particular in its temporal aspect. But it is not always true that the dynamic aspect of the simulation imitates the temporal aspect of the target system. Some CS can be said to be *mimetic in their results* but *non-mimetic in their trajectory* [51].

A partially similar distinction is evoked by [56]. In fact, we have to distinguish simulations of which the trajectory tends to be temporally mimetic from other simulations that are tricks of numerical calculus. These tricks enable to attain the result without following a trajectory similar to the one either of the real system, or of the apparent temporal (historical) aspect of the resulting pattern of the simulation. For instance, it is possible to simulate the growth of a botanical plant sequentially and branch by branch (through a non-mimetic trajectory) and not through a realistic parallelism, i.e. burgeon by burgeon (through a mimetic trajectory), and to obtain the same resulting and imitating image [51]. Thereafter, the resulting static image can be interpreted by the observer as a pattern which has an evident temporal (because historical) aspect, clearly visible from the arrangement of its branching structure. But this observer has no way to know whether this imitated historical aspect has been obtained through a really mimetic temporal approach or not. But either was a simulation process.

The same remark stands for Social Sciences. If we distinguish between “historical genesis” and “logical genesis, the processes are not the same. The logical genesis progresses along an abstract / a-historic succession of steps, with no intrinsic temporality.

So, depending on its kind, a simulation doesn’t have always to be founded on the direct imitation of the temporal aspect of the target system. It depends on what is first simulated or ... imitated. It is a bit frustrating to see that the temporal aspect is itself dependent on the persistent - but vague - notion of imitation or similitude. Surely, it remains most of the time correct and useful to see a CS as an imitating temporal process originally founded on a mathematical model. It is a convenient definition

because the notion of similitude is only alluded to. This definition remains correct when it suffices to analyze the relations between a classical implementation of a unique model and its computational instantiation on a computer (“simulation of model”).

But it becomes very restrictive - and sometimes false - when we consider the variety of contemporary CS strategies. Today, there exist various kinds of CS of the same model or of different systems of submodels. As a result, in order to characterize a CS, are we condemned to rehabilitate the old notion of similitude which Goodman [20], among others, shows to be very problematic because very relativistic itself? Are we condemned to the classical puzzle caused - as shown again by Winsberg [56] - by a dualistic position assuming that there are only two types of similarities at stake in an experiment or a simulation: formal or material (Guala [25])?

2.2. Subsymbols and denotational hierarchy in simulations

In fact, following Varenne [51, 52], it is possible to give a minimal characterization of a CS (not a definition) *referring neither to an absolute similitude (formal or material) nor to a dynamical model.*

First, let's say that a *simulation* is minimally characterized by a *strategy of symbolization* taking the form of at least one step by step treatment. This step by step treatment proceeds at least in *two major phases*:

1st phase: a certain amount of operations *running on symbolic entities (taken as such) which are supposed to denote* either real or fictional entities, reified rules, global phenomena, etc.

2nd phase: an observation or a measure or any mathematical or computational *re-use* (e.g., in CSs, the simulated “data” taken as data for a model or another simulation, etc.) of the result of this amount of operations *taken as given* through a visualizing display or a statistical treatment or any kind of external or internal evaluations.

In analog simulations, for instance, some material properties are taken as symbolically denoting other material properties. In this characterization, the external entities are said “external” as they are external to the systems of symbols specified for the simulations, whether these external entities are directly observable in empirical reality or are fictional or are holistic constructs (such as a “rate of suicide”).

Because of these two distinct and major phases in any simulations, the symbolic entities denoting the external entities can be said to be used in a classical *symbolic* way (as in any calculus), but also in a *subsymbolic* way. Smolensky [45] coined the term “subsymbol” to designate those empirical entities processing in a connectionist network at a lower level and which aggregation can be called a symbol at an upper level. They are constituents of symbols: “they participate in numerical – not symbolic – computation” (p.3). Berkeley [6] has recently shown that Smolensky’s notion has to be interpreted in regard to a larger scale and from an internal relativistic point of view. This *relativity of symbolic power* is what we want to express through our relativistic use of the term.

In a simulation, the symbolic entities are denoting (sometimes through complex routes of reference). They are symbols as such. But, it is some global result of their

interactions which is of interest, during the second phase. During this evaluation phase, they are treated at another level than the one at which they first operated. They were first treated as symbols, each one denoting at a certain level and through a precise route of reference. But they finally are treated *as relative subsymbols*.

Indeed, simulation is a process, as it is often said. But it is more characteristically a way of partially using entities taken as symbols in a less *convention-oriented* fashion and with less *combinatorial power* [5], i.e. with more “independence to any individual language” [12], comparatively to other levels of systems of symbols.

So, we define here a *sub-symbolization* as a strategy to use symbols for a *partial “iconic modeling”* [14]. Contrary to what could be said in 1961, not all simulations are “iconic modeling” in the sense of the iconicity images can have. But they present at least some level of *relative iconicity*. Fischer [12] defines “iconicity” as “a natural resemblance or analogy between a form of a sign [...] and the object or concept it refers to in the world or rather in our perception of the world”. She insists on the fact that not all iconicities are *imagic* and that an iconic semiotic relation is relative to the standpoint of the observer-interpreter. What is the most important is this property of an iconic relation to be - *relatively to a given language or vision of the world - less dependent of this language*.

Let us say now that a CS is a simulation for which we delegate (at least) the first phase of the step by step treatment of symbolization to a digital and programmable computer.

Usually, with the progress in power, in programming facilities and in visualizing displays, computers are used for the second phase two. At any rate, all kinds of CS make use of, at least, one kind of *subsymbolization*.

Note that the symmetrical relations of *subsymbolization* and *relative iconicity* entail a representation of the mutual relations between levels of signs in a CS which is similar to the *denotational hierarchy* presented by Goodman [21]. For Goodman, “reference” is a general term “covering all sorts of symbolization, all cases of standing for”. Denotation is a kind of reference: it is the “application of a word or a picture or other label to one or many things”.

There is a hierarchy of denotations: “At the bottom level are nonlabels like tables and null labels as ‘unicorn’ that denote nothing. A label like ‘red’ or ‘unicorn-description’ or a family portrait, denoting something at the bottom level is at the next level up; and every label for a label is usually one level higher than the labeled level” ([21], p. 127). For Goodman, an ‘unicorn-description’ is a ‘description-of-an-unicorn’ and not a description of an unicorn, because it is a particular denoting symbol which denotes nothing really existing.

There are many kinds of denotation. Goodman [20] subsumes mathematical modeling and computational treatment in a kind called “notation”. Contrary to what happens in a system of pictorial denotation, in notations, symbols are “unambiguous and both syntactically and semantically distinct”. Notation must meet the requirements of “work-identity in every chain of correct steps from score to performance and performance to score”. For instance, the western system for writing music tends to be a notation. Many authors who assume that a kind of formal analogy - and nothing else - must be at stake in a CS (which they often reduce to a calculus of a uniform model) do implicitly agree with this reduction of CS to a system of notation.

But, in fact, many simulations present a variety of notations. No unique notation governs them. Moreover, many CS have symbols operating without having been given any clear semantic differentiation (for instance, those CS which are computational tricks to solve a model manipulate discrete finite elements which have no meaning or no corresponding entities in the target system) nor stable (absolute) semantic during the process itself (e.g. in some multileveled complex simulations).

Following Goodman [20] on symbols, but reversing his specific analyses on computational models, we can say that, in a numerical simulation of a fluid mechanics' model, e.g., each operating subsymbol is a denotation-of-an-element-of-the-fluid but not a denotation of an element of the fluid. During the course of a computation, the same level of symbol (from the implementer point of view) can be taken either as iconic or as symbolic, depending on the level at which the event or operation considers the actual elements.

It is not possible to show here in details the various *routes of reference* that are used in various CS. It suffices to say that, whether a simulation or an experiment finally is successful or not, simulationists and experimenters first ought to have a representation of the *denotational hierarchy* and *then of the remoteness of the references of the symbols they will use or will let use* (by the computer).

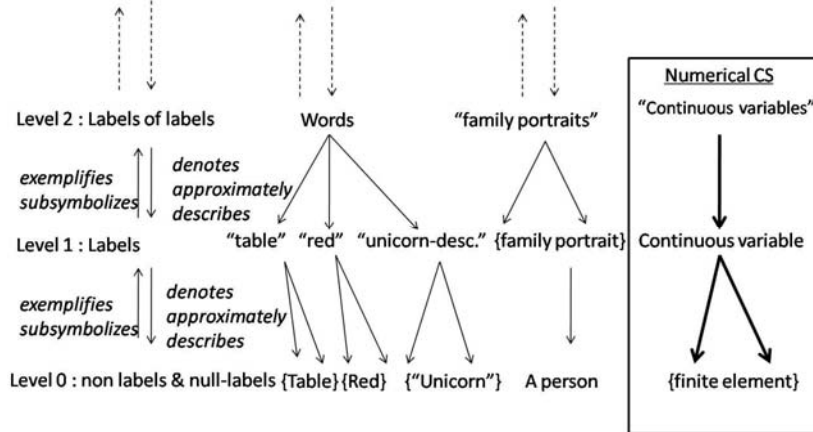


Figure 1: the denotational hierarchy and its relative subsymbols

Figures 1 & 2 can help to follow instances of such routes by following successive arrows between levels of symbols. Figure 1 represents (1) the levels, (2) some of Goodman's examples, (3) the first kind of CS we propose to insert in this hierarchical interpretation and (4) the types of semiotic relations between things and/or symbols across levels.

Figure 2 shows the insertion of Agent-Based CS. The analysis surely can be refined. E.g., the place of such a CS can be expanded or changed in the hierarchy, but not the kinds of local relations between levels of symbols at stake. What is important is that the relative position between symbols is preserved. Accordingly, figure 2 shows the correlative degrees of *combinatorial power* and *iconicity* across levels. We image it through a deforming black quadrilateral (which tends to possess a constant

surface): *the more important the iconic aspect of the symbol is, the less its combinatorial power is.*

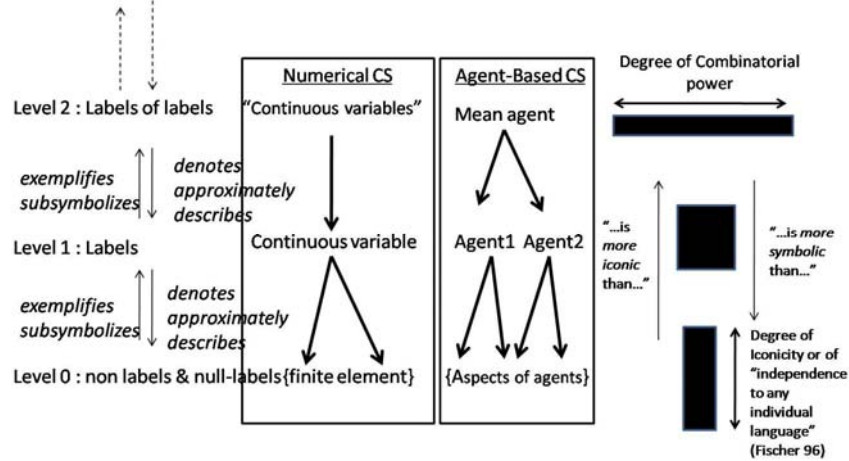


Figure 2: Degree of *combinatorial power* and degree of *iconicity*

In front of this new way of representing the referential relations between symbols in CS and between things (or facts, etc.) and symbols, we can see that Winsberg [56] is perfectly right when he says that the dualistic approach is too simple and puzzling. But he is too rapid when he directly goes back to an *epistemology of deference* instead of trying a *careful and differentiating epistemology of reference*. Contemporary epistemology of deference remains a restrictive philosophy of knowledge because it persists to see any symbolic construct produced by sciences - and their instruments - as analogue to human knowledge: i.e. as *propositional*, such as a belief ("S believes that *p*"). So, its ability to offer any new differentiating focuses on CS, especially between models and simulations and - what seems so crucial today - between *kinds of simulations*, sounds very doubtful.

The puzzle concerning the empirical or conceptual status of CSs largely stems from this large and simplistic reduction of any CS to a notation and, through that, to a formal language always instantiating some "propositions" analogous to "musical sentences" performed through a unique system of notation.

Our characterization gives the possibility *to stay at the level of the symbols* a stake, and not to jump prematurely to propositions, this *without going back to a naïve vision of an absolute iconicity of simulations*. Iconicity does not entail absolute similitude nor materiality. It is a relativistic term. E.g., in cognitive economics [53, 54], agent-based simulations can be said to operate on some *iconic signs* because they denote directly - term to term, so with a *weak dependence on linguistic conventions* - some credible rule of reasoning.

2.3. Three kinds of Computer Simulations

Following this characterization, it is possible to go further and distinguish at least three kinds of CS depending on the *kinds of subsymbolization at stake*:

- 1- a CS is *model-driven* (or *numerical*) when it proceeds from a subsymbolization of a given model. That is: the model is treated through a discrete system which still can be seen as a system of notation.
- 2- a CS is *rule-driven* (or *algorithmic*) when it does not proceed from the subsymbolization of a previous mathematical model. Rules are now constitutive. The rules of the algorithm are subsymbolic regarding some hypothetical algebraic or analytical mathematical model and they are iconic regarding (relatively to) the formal hypotheses implemented (e.g. “stylized facts”). Hence, from the point of view of the user, an iconic aspect still appears in such a simulation. And this iconicity serves as another argument to speak about experiment in another sense. As underlined by Sugden it is precisely the case of Schelling’s model: causal mechanisms are denoted through partial and relative iconic symbols. Those elementary mechanisms - which are elementary denoted in the CS - are what is “empirically” assessed here. It is empirical to the extent that there is no theory of the mass-behavior of such distributed mechanisms. So, the symbols denoting this mechanism operate in a poor symbolic manner: they have a weak combinatorial power, and a weak ability to be directly condensed and abridged in a symbolic manner. *Experience* (passive strategy of observation) is convoked there, rather than *experiment* (an interactive strategy of interrogation and observation).
- 3- a CS is *object-driven* (or *software-based*) when it first proceeds not from a given uniform formalism (either mathematical or logical) but from various kinds and levels of denoting symbols which symbolicity and iconicity are internally relative and depend on internal relations between these kinds and levels. Most of the time (but not necessarily), such simulations are based on multi-agents systems implemented by agent- / object-oriented programming so as to enable the representation of various degrees of *relative reifications* - or, conversely, *relative formalizations* - of objects and relations.

Concerning the first kind, the focus is on the model. Then scholars are willing to say that they are *computing the model*, or, at most, that they are *experimenting on the model*. We have seen that a symbol-denoting-an-element-of-the-fluid is not necessarily a symbol denoting anything. It can be a *null-label* which nevertheless possesses some residual (weak) combinatorial power which can be worked upon once placed in the conditions of some machine delegated computational iterations (CS).

In the case of *algorithmic CS*, scholars often say that their list of rules is a “model of simulation” and that they make with it a “simulation experiment”. They say that because the iconicity of the subsymbols is directly linked to a familiar level of empirically oriented consideration of the system.

The recent emergence of complex multidisciplinary and/or multi-levelled CS has given rise to mix CS: some of their operations are considered as calculus of models, whereas some others are algorithmic and not far from being iconic to some extent, while others are only exploitations of digitalizations of scenes (such as CS coupled to Geographic Information Systems).

From this standpoint, a software-based simulation of a complex system often is a simulation of interacting pluri-formalized models. The technical usefulness of such a CS is new [51]. It relies no more on the practical calculability of one intractable model but on the *co-calculability* of heterogeneous - from an axiomatic point of view - models. E.g.: CS in “artificial life”, CS in computational ecology, CS in post-genomic developmental biology, CS of interrelated process in multi-models, multi-perspective CS...

2.4. Types of empiricity for Computer Simulations

Varenne [51] has shown that 4 criteria of empiricity, at least, can be used for a CS according to this characterization.

- 1- when focusing on a partial or global result of the CS to see some kind of similarity of this result (this similarity being interpreted in terms of relative iconicity, formal analogy, exemplification or identity of features), and when the result is found to denote some target system, we can speak of an *empiricity of the CS regarding the effects*. The focus relies here on the second phase of the simulation. Once seen from the global results, the elementary symbols - which first operated - are overlooked and treated as subsymbols.
- 2- when focusing on the partial iconic aspects of some of the various types of elementary symbols operating in the computation, we can speak of some *empiricity of the CS regarding the causes*. The focus relies here on the first phase of the CS and on the supposed realism or credibility of these elements with respects to the target system.

Both of these dimensions of empiricity have been evoked by Galison [17] in the case of numerical simulations, but not the two others to come. Both concern the external validity of the simulation in the sense of Guala. Note that they are similar to that kind of non interactive experiment called “experience” for which observation suffices.

- 3- when focusing on the intrication of levels of denotations operating in a complex pluriformalized CS, it is possible to decide that there is an intellectual opacity different in nature from the one coming from a classical intractability. We can speak then of an *empiricity regarding the intrication of the referential routes*. Such an empiricity (as the 4th) does not come from the existence of a rather passively experienced level of symbols as in (1) or (2). But it comes from an active comparison between different iterative intrications of levels of symbol, be they controlled (semantically or instrumentally) or uncontrolled factors in this virtual experiment.
- 4- when focusing on the intrication of the resulting epistemic status of such a complex CS with levels of models and then levels of denotational systems, a 4th kind of empiricity comes to view. It is a problem because not only each of its level has its own form, that is, its own alphabet and rules of (weak or strong) combination, but each one has a different denotational level or position in the hierarchy too. So, each one can entail for itself a different route back to reference.

Each one can have a different epistemic status in that it belongs to a different “world” [22], the one being fictional, the other descriptive, the other explanative. We can speak here of *an empiricity regarding the defect of any a priori epistemic status*. That is: the CS has to be treated - first and *a minima* - as an experiment because we do not know *a priori* if it is an experiment for any of the 3 other reasons, or a theoretical argument, or only a conceptual exploration. Moreover, it is probable that *there exists no general composition law of epistemic statuses for some of such complex CS and that they demand a case-by-case epistemological investigation, with the help of careful denotational analyses*.

2.5. Models, simulations and kinds of experiment

Now that we have gained some conceptual tools, let’s rapidly but accordingly reinterpret some of the different epistemological positions we first put into perspective in sect. 1.

How and to what extent models can be seen as some kind of experiment?

Facing some cases, like Schelling’s model discussed by Sugden, we can say that a model has an empirical dimension in itself because *some causal factors are denoted through symbols of which partial iconicity is patent and can be reasonably recognized* as a sufficiently “realistic” conjecture in the argumentative approach of the “credible world”.

On the contrary, models are *seen from an instrumentalist standpoint when the level of iconicity of their symbols is weak* (the remoteness of reference is important) and when this is *their combinatorial power at a high level in the denotational hierarchy which is requested* (i.e. Friedman’s unrealism of assumption argument). Retrospectively, such an epistemology can be seen as a contingent rationalization of some limited mono-leveled formalizations (which were the only one available in the past) in contrast to the current more complex and developed abilities to vary routes of reference through ABM and computer-aided simulations.

The notion of “stylized fact” is ambiguous in this concern because it can serve to put the emphasis either on the stylization, or on the factuality and then on the eventual iconicity of the used symbolization. The fact is that, independently of *an explicit commitment toward a denotational hierarchy*, models of “stylized facts” cannot be said *a priori* to be “conceptual exploration” or “experiments”.

How and why can a CS be seen as an experiment on a model?

As a CS entails some kind of subsymbolization, every CS of a model treats a model at a sublevel which tends to make its relation to the model analogous to the naïve dualistic relation between the formal constructs and the concrete reality. Because of this analogy of relations between two levels of different denotational authority (no matter what these levels are), *such a CS can be said to be an experiment on the model*. But if we focus on some symbolic aspects of used subsymbols, we can speak of such a CS of model as *a conceptual exploration*.

It follows that the *external validity* is a matter of degree and depends on the strength of the *alleged iconic aspects*. If this iconic aspect is extremely stabilized and

characterized, the simulation can even be compared to an *exemplification*. In this case, external validity is not far from an internal one.

To what extent a CS can be seen as an experiment in itself?

There are at least 4 criteria to decide whether a simulation is not only an experiment *on* the model but an experiment *in itself*. A CS can first lend its empiricity from an *experiencing*, that is, from a comparison with the target (external validity): and those are (1) the *empiricity regarding the causes* (of the computation) and (2) the *empiricity regarding the effects* (of the computation). But its empiricity can be decided not from an experiencing of a more or less direct route of reference but from a real *experimenting* on the interaction between levels of symbols, i.e. with controlled and uncontrolled changing factors: and here are (1) the *empiricity regarding the intrication of the referential routes*, and (2) the *empiricity regarding the defect of any a priori epistemic status*.

From this standpoint, through this particular experimenting dimension, software-based CS gain some particular kind of empiricity which gives them a similar *epistemic power* (pace Morgan) than ordinary experiments.

Conclusion

The coming years will see the expansion of more empirically based CS with agents in social sciences (as in all the sciences of complex systems), and of multidisciplinary CS, especially between social sciences and biology or ecology. Due to differences in methodological habits, epistemological misunderstandings between disciplines will probably increase. So, we think that *careful attention to the multiplicity of standpoints on symbols, on their mutual relations* and on the *implicit routes of references* operated through them by computations will help to discern more precisely the denotational power, hence the epistemic status and credibility of such complex models and simulations. In this concern, this paper has presented a first outline of conceptual and applicative developments in the domain of an *applied, referentialist but multi-level centered epistemology of complex models and simulations*.

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